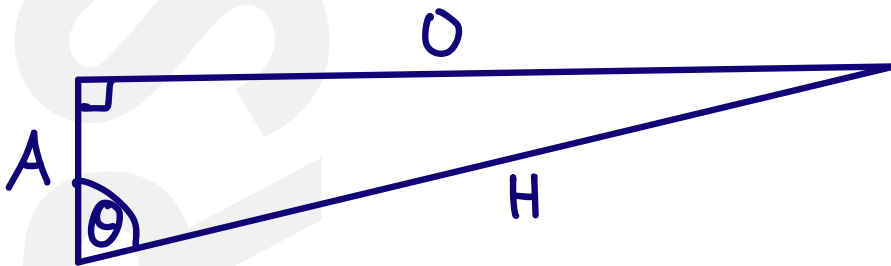


1. Calculate the **angle**,  $\theta$ , in a triangle with a hypotenuse of length 1.2 m and an opposite side length of 1.0 m.



$$\sin \theta = \frac{O}{H}$$

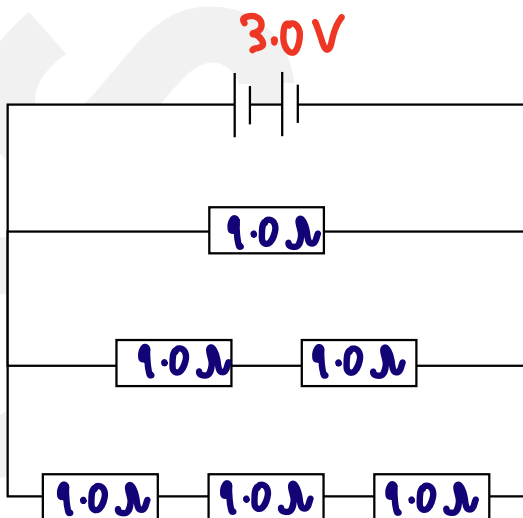
$$\theta = \sin^{-1} \left( \frac{1.2}{1.0} \right) = \underline{56^\circ}$$

2. Write down the **units** for:

- a. Potential difference
- b. Resistivity
- c. Capacitance
- d. Momentum
- e. Electromotive force
- f. Magnetic flux density

volt, V  
ohm metre,  $\Omega m$   
farad, F  
 $kg m s^{-1}$   
volt, V  
tesla, T

3. In the circuit below are six identical  $9.0 \Omega$  resistors and a battery of e.m.f 3.0 V. Calculate the total **energy transferred per second** in this circuit.



$$\frac{1}{R_T} = \frac{1}{9.0} + \frac{1}{(9.0+9.0)} + \frac{1}{(9.0+9.0+9.0)}$$

$$R_T = 4.909$$

$$P = \frac{V^2}{R_T} = \frac{3.0^2}{4.909} = 1.833 \approx \underline{1.8 W}$$

# 2<sup>nd</sup> November – Part 1

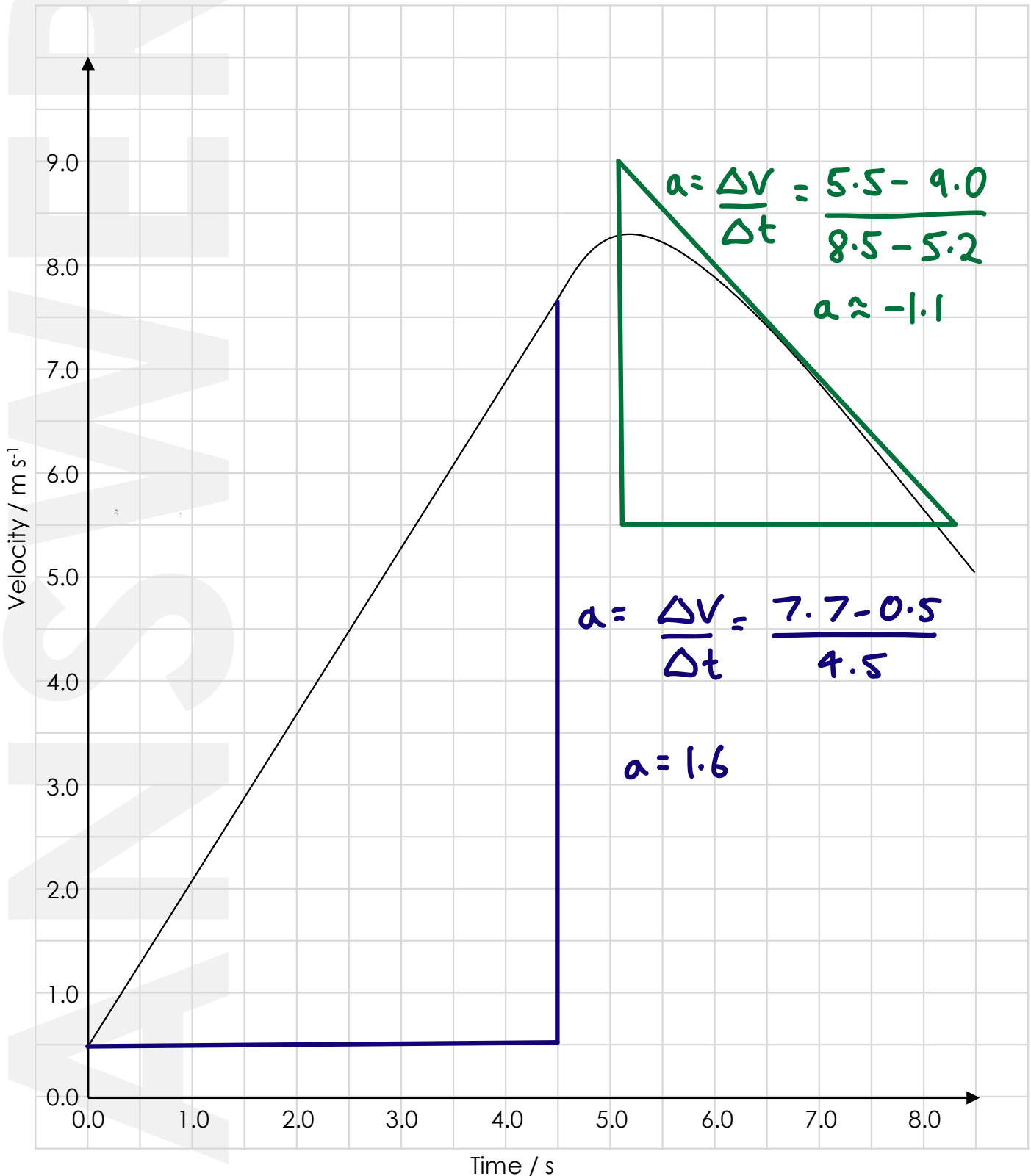
1. Calculate the **acceleration** at:

a.  $t = 2.0$  s

$$a = \underline{1.6} \text{ m s}^{-2}$$

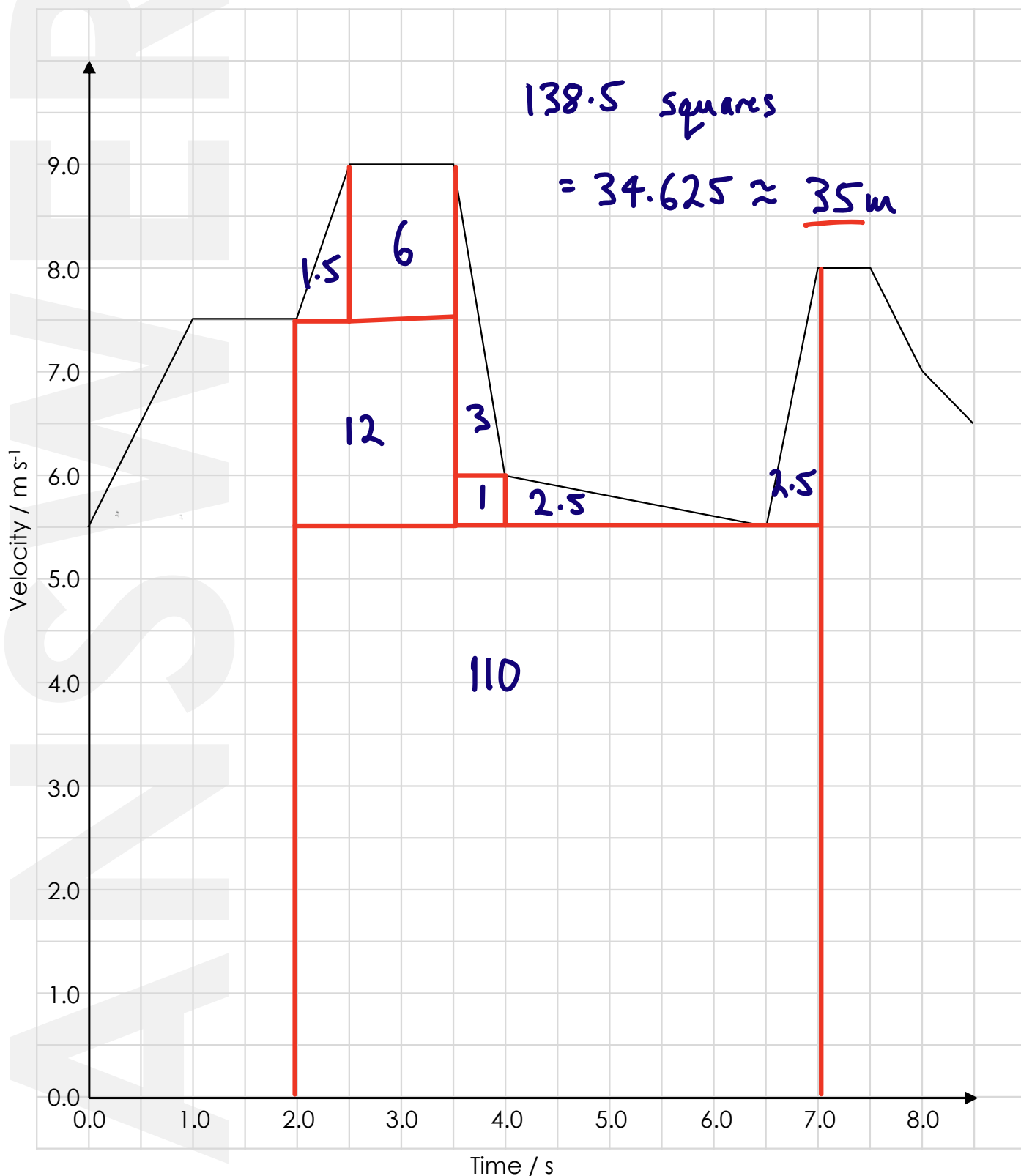
b.  $t = 6.5$  s

$$a \approx \underline{-1.1} \text{ m s}^{-2}$$



# 2<sup>nd</sup> November – Part 2

2. Calculate the **displacement** between  $t = 2.0$  and  $t = 7.0$  s.



## Percentage Uncertainty – Single Measurement

The percentage uncertainty for a single measurement can be calculated from the absolute uncertainty (which is often stated in exam questions) and the measured value.

$$\text{percentage uncertainty} = \frac{\text{absolute uncertainty}}{\text{measured value}} \times 100\%$$

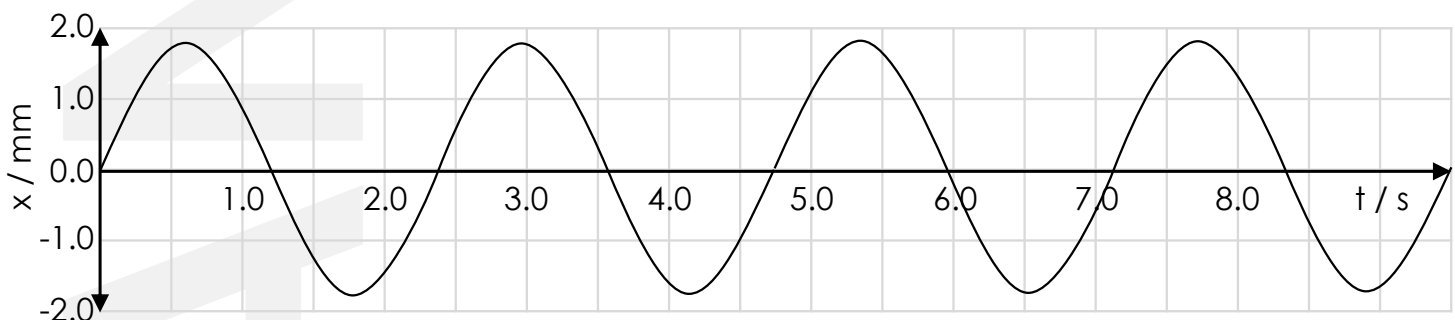
Example: Calculate the percentage uncertainty in the length of a pencil measured with a value of  $12.2 \pm 0.1$  cm.

$$\text{percentage uncertainty} = \frac{0.1}{12.2} \times 100\% = 0.820 \approx 0.82\% \text{ (2 s.f.)}$$

1. Calculate the **percentage uncertainty** (to 2 s.f.) in the following data:

	Measured Value	Absolute Uncertainty	Percentage Uncertainty / %
a.	15 mm	$\pm 1$ mm	6.7
b.	272 mm	$\pm 1$ mm	0.37
c.	8.21 s	$\pm 0.01$ s	0.12
d.	8.21 s	$\pm 0.2$ s	2.4
e.	2.8 kg	$\pm 0.1$ kg	3.6
f.	2.802 kg	$\pm 0.001$ kg	0.036

2. Determine the **amplitude** and **time period** of the following wave.



$$A = \underline{1.8 \text{ mm}}$$

$$T = \frac{9.5}{4} = 2.375 \approx \underline{2.4 \text{ s}}$$

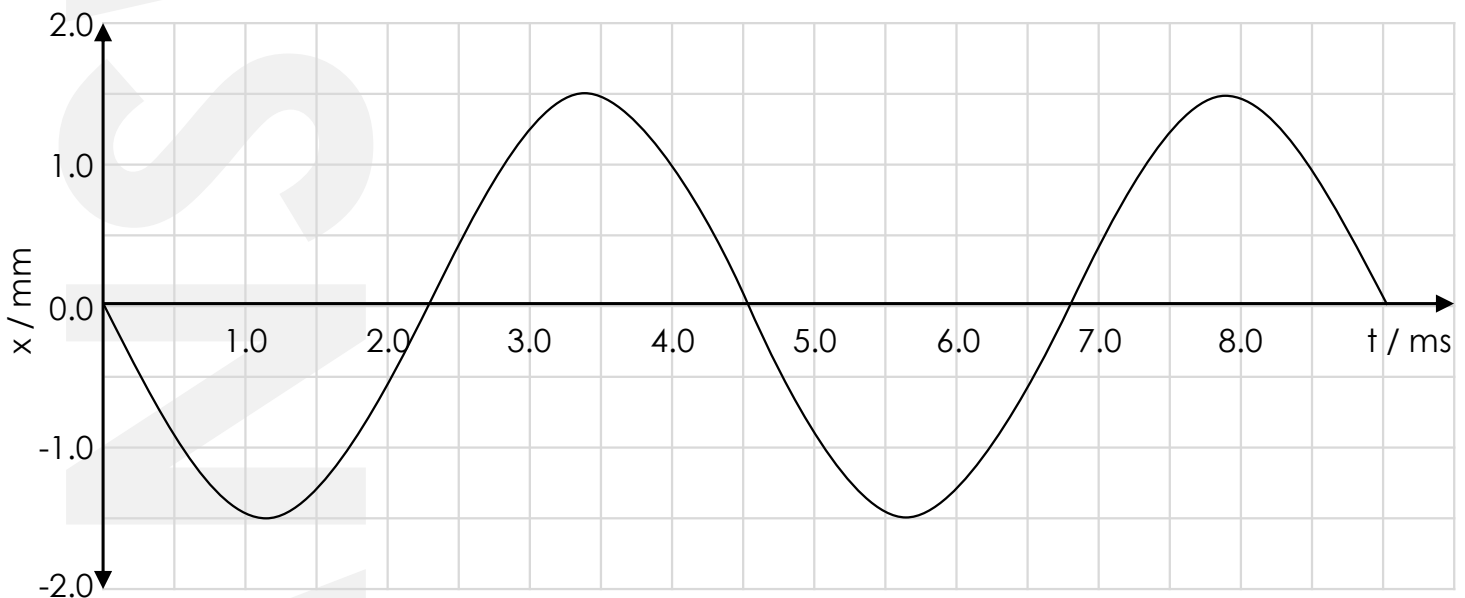
1. Calculate the **percentage uncertainty** (to 2 s.f.) in the following data:

	Measured Value	Absolute Uncertainty	Percentage Uncertainty / %
a.	10 mm	$\pm 1$ mm	10
b.	10.14 mm	$\pm 0.01$ mm	0.099
c.	8.2 cm	$\pm 1$ mm	1.2
d.	0.882 m	$\pm 1$ mm	0.11
e.	0.8 s	$\pm 0.1$ s	13
f.	8.2 s	$\pm 0.1$ s	1.2

2. **Define** Ohm's law.

The potential difference across a component is directly proportional to the current through it, at a constant temperature.

3. Determine the **amplitude**, **time period** and **frequency** of the following wave.

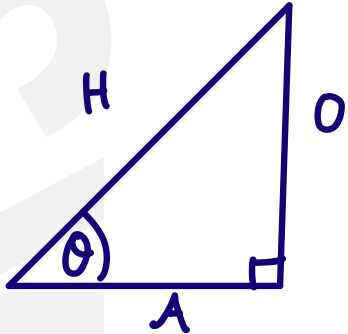


$$A = \underline{1.5 \text{ mm}}$$

$$T = \underline{4.5 \text{ ms}}$$

$$f = \frac{1}{4.5 \times 10^{-3}} = \underline{2.2 \times 10^2 \text{ Hz}}$$

1. Calculate the **angle**,  $\theta$ , in a triangle with a hypotenuse of length 6.5 cm and an adjacent side length of 3.1 cm.



$$\cos \theta = \frac{A}{H}$$

$$\theta = \cos^{-1}\left(\frac{3.1}{6.5}\right) = \underline{62^\circ}$$

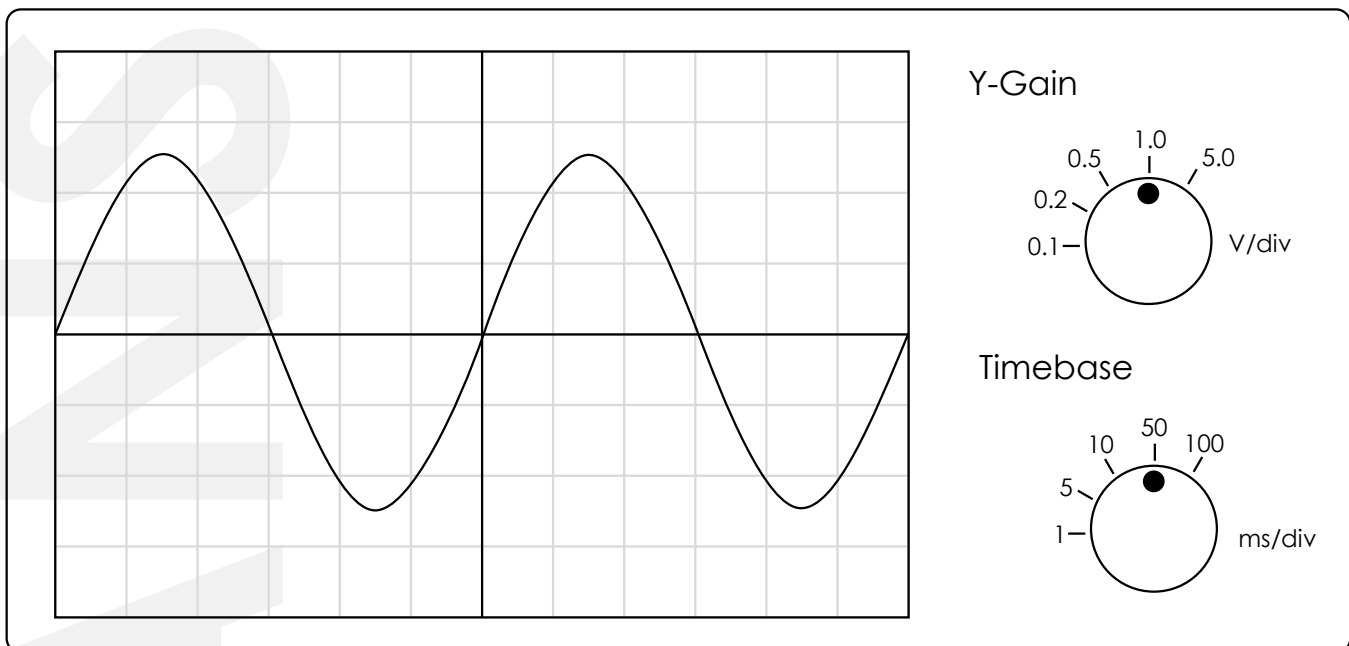
2. When investigating resistivity, a wire is used that has its diameter of 0.42 mm measured with a micrometer to  $\pm 0.01$  mm, and length of 40.0 cm measured with an uncertainty of  $\pm 1$  mm.

Calculate the **percentage uncertainty** (to 2 s.f.) in:

a. The **diameter**  $\frac{0.01}{0.42} \times 100 = \underline{2.4\%}$

b. The **length**  $\frac{1}{400} \times 100 = \underline{0.25\%}$

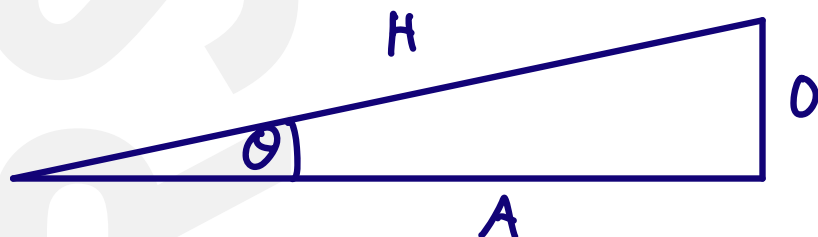
3. Determine the **amplitude** (in V) and **time period** of the signal on this oscilloscope trace.



$$A = 2.5 \times 1.0 = \underline{2.5V}$$

$$T = 6.0 \times 50 \times 10^{-3} = \underline{0.30s}$$

1. Calculate the **length** of the adjacent side of a right angle triangle with an angle of  $10^\circ$  and an opposite side length of 9.3 cm.



$$\tan \theta = \frac{O}{A}$$

$$A = \frac{9.3}{\tan 10} = \underline{53 \text{ cm}}$$

2. Laser light is incident on a double slit and projected onto a screen. The total distance across eleven fringes of light is measured with a ruler as 5.4 cm, with an uncertainty of  $\pm 1 \text{ mm}$ .



- a. Calculate the **percentage uncertainty** (to 2 s.f.) in the distance measured

$$\frac{1}{54} \times 100 = \underline{1.9\%}$$

- b. Calculate the **spacing** between each fringe

$$\frac{54}{10} = \underline{5.4 \text{ mm}}$$

- c. State the **percentage uncertainty** in spacing between fringes

$$\underline{1.9\%}$$

3. Define:

a. **Wavelength** The distance between two adjacent points that are in phase.

b. **Monochromatic light** Light that has a single wavelength.

c. **Coherent waves** Waves that have a constant phase difference.

1. Calculate the **mean value**, and **range**, of the following numbers:

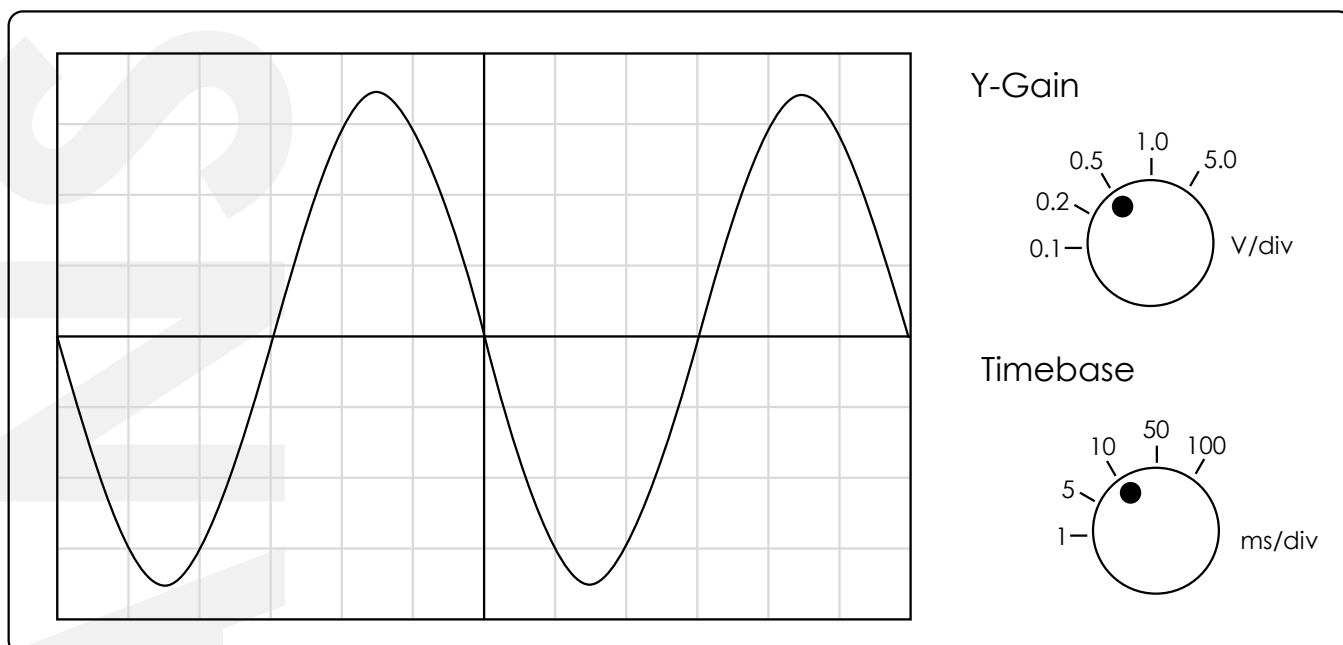
	Value 1	Value 2	Value 3	Value 4	Value 5	Mean	Range
a.	82.57	85.48	86.06	85.76	85.29	<b>85.03</b>	<b>3.49</b>
b.	17.94	16.82	16.23	16.28	16.57	<b>16.77</b>	<b>1.71</b>
c.	9.95	8.04	9.32	8.56	9.00	<b>8.97</b>	<b>1.91</b>
d.	3.50	3.57	3.62	3.41	3.43	<b>3.51</b>	<b>0.21</b>

2. The wavelength of light is investigated using a double slit. The slit separation is measured using a travelling microscope as  $0.60 \pm 0.01$  mm.

Calculate the **percentage uncertainty** (to 2 s.f.) in this measurement.

$$\frac{0.01}{0.60} \times 100 = \underline{1.7\%}$$

3. Determine the **amplitude** (in V) and **frequency** of the signal on this oscilloscope trace.



$$A = 3.5 \times 0.5 = 1.75 \approx \underline{1.8 \text{ V}}$$

$$f = \frac{1}{T} = \frac{1}{6 \times 10 \times 10^{-3}} = 16.66 \approx \underline{17 \text{ Hz}}$$



1. Calculate the **mean value**, and **range**, of the following numbers:

	Value 1	Value 2	Value 3	Value 4	Value 5	Mean	Range
a.	83.53	84.85	86.06	82.66	85.29	<b>84.48</b>	<b>3.4</b>
b.	84.35	84.46	84.56	84.47	84.55	<b>84.48</b>	<b>0.21</b>
c.	1.85	1.04	1.32	1.56	1.23	<b>1.40</b>	<b>0.81</b>
d.	23.53	23.47	23.61	23.14	23.40	<b>23.43</b>	<b>0.47</b>

2. To investigate the Young modulus of a material like copper, a thin piece of wire can be loaded so it extends.

The diameter of wire used in this experiment is measured with a micrometer screw gauge as  $0.42 \pm 0.01$  mm.

- a. Calculate the **percentage uncertainty** (to 2 s.f.) in the diameter

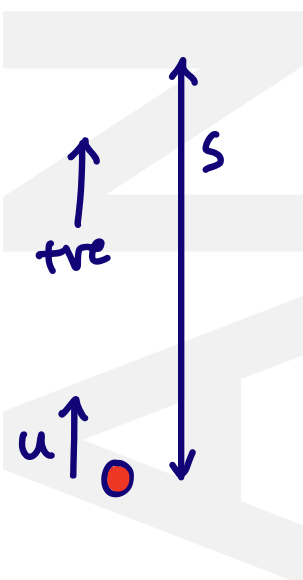
$$\frac{0.01}{0.42} \times 100 = \underline{2.4\%}$$

- b. State the **percentage uncertainty** (to 2 s.f.) in the radius

$$\underline{2.4\%}$$

3. A ball is thrown vertically up into the air with an initial velocity of  $5.0 \text{ m s}^{-1}$ . Calculate how **long** the ball takes to return to the start position.

State any assumptions made in your answer.



$$\begin{aligned} S & \\ u &= 5.0 \text{ m s}^{-1} \\ v &= 0 \text{ m s}^{-1} \\ a &= -9.81 \text{ m s}^{-2} \\ t &= ? \end{aligned}$$

$$t = \frac{v-u}{a} = \frac{0-5.0}{-9.81}$$

$$t = 0.5097$$

$$\therefore t_{\text{total}} = 2 \times 0.5097 = \underline{1.0 \text{ s}}$$

Assume no air resistance

## Percentage Uncertainty – Repeat Measurements

The percentage uncertainty for repeated measurements can be calculated from the uncertainty, which is equal to half the range, and the mean value.

$$\text{percentage uncertainty} = \frac{\text{half the range}}{\text{mean value}} \times 100\%$$

Example: Calculate the percentage uncertainty in the following set of data:

d / mm	23.4	22.9	23.1	23.3
--------	------	------	------	------

$$\text{half the range} = (23.4 - 22.9) \div 2 = 0.25$$

$$\text{mean value} = (23.4 + 22.9 + 23.1 + 23.3) \div 4 = 23.175$$

$$\text{percentage uncertainty} = \frac{0.25}{23.175} \times 100\% = 1.08 \approx 1.1\% \text{ (2 s.f.)}$$

1. Calculate the **percentage uncertainty** (to 2 s.f.) in the following data:

	Value 1 / mm	Value 2 / mm	Value 3 / mm	Value 4 / mm	Value 5 / mm	Mean / mm	½ Range / mm	Percentage Uncertainty / %
a.	83	84	87	81	86	84.2	3.0	3.6
b.	83	85	84	84	85	84.2	1.0	1.2
c.	1.35	1.24	1.32	1.36	1.23	1.30	0.065	5.0
d.	0.25	0.24	0.26	0.21	0.23	0.238	0.025	11

2. A cheetah accelerates from rest to a velocity of  $22 \text{ m s}^{-1}$  in a time of 3.5 seconds.

Calculate how **far** it has travelled in this time.

$$s = ?$$

$$u = 0 \text{ m s}^{-1}$$

$$v = 22 \text{ m s}^{-1}$$

$$a =$$

$$t = 3.5 \text{ s}$$

$$s = \frac{1}{2}(u+v)t$$

$$s = 0.5 \times (0 + 22) \times 3.5 = 38.5$$

$$\approx \underline{\underline{39 \text{ m}}}$$

1. Calculate the **percentage uncertainty** (to 2 s.f.) of the following data:

	Value 1 / mm	Value 2 / mm	Value 3 / mm	Value 4 / mm	Value 5 / mm	Mean / mm	½ Range / mm	Percentage Uncertainty / %
a.	127	130	132	128	128	129	2.5	1.9
b.	138	135	<del>84</del>	136	132	135.25	3.0	2.2
c.	2.65	2.68	2.68	2.66	2.64	2.662	0.02	0.75
d.	0.61	0.61	0.62	0.65	0.63	0.624	0.02	3.2

2. Define:

a. **Kirchhoff's first law**

$$\sum I_{in} = \sum I_{out} \quad (\text{at a junction})$$

b. **Kirchhoff's second law**

$$\sum E = \sum V \quad (\text{around any closed loop})$$

3. You are given the equation 'energy = momentum x the speed of light'. Work out whether this is **homogeneous** or not.

Note: An equation is homogenous if the units on both sides of the equals sign are the same.

$$E = pc$$

$$E = \frac{1}{2}mv^2 = [\text{kg}] \times [\text{m s}^{-1}]^2 = [\text{kg m}^2 \text{s}^{-2}]$$

$$p = [\text{kg m s}^{-1}]$$

$$pc = [\text{kg m s}^{-1}] \times [\text{m s}^{-1}]$$

$$c = [\text{m s}^{-1}]$$

$$pc = [\text{kg m}^2 \text{s}^{-2}]$$

Yes it is

1. Define a:

a. **Progressive** wave

*Transfers energy.*

b. **Transverse** wave

*Oscillations at 90° to the direction of energy transfer.*

2. While investigating standing waves on a string, the distance between adjacent nodes was measured as 22.0 cm with an uncertainty of  $\pm 0.4$  cm owing to the difficulty in identifying exactly where the position of each node was.

a. Calculate the **percentage uncertainty** (to 2 s.f.) in this measurement.

$$\frac{0.4}{22.0} \times 100 = \underline{1.8\%}$$

b. State the **percentage uncertainty** in the calculated wavelength of the standing wave (the distance from a node to a node is equal to half the wavelength).

*1.8%*

3. A van of mass 4500 kg undergoes a collision where it decelerates from an initial velocity of  $12.0 \text{ m s}^{-1}$  to a final velocity of  $4.0 \text{ m s}^{-1}$  in a time of 400 ms.

Calculate the **average force** experienced during the collision.

$$F = \frac{\Delta p}{\Delta t} = \frac{m(v-u)}{t} = \frac{4500(4.0-12.0)}{400 \times 10^{-3}}$$

$$F = \underline{90\,000 \text{ N}}$$

1. Determine the **result** that should be recorded for X and calculate the **percentage uncertainty** in the data:

X / mm	0.38	0.42	0.41	0.41	0.42
--------	------	------	------	------	------

$$X = \underline{0.41 \text{ mm}}$$

$$\frac{0.02}{0.408} \times 100 = \underline{4.9\%}$$

2. In a further experiment to investigate standing waves on a string, the distance between five nodes was measured as 88.3 cm, again with an absolute uncertainty of  $\pm 0.4$  cm owing to the difficulty in identifying exactly where the position of each node was.

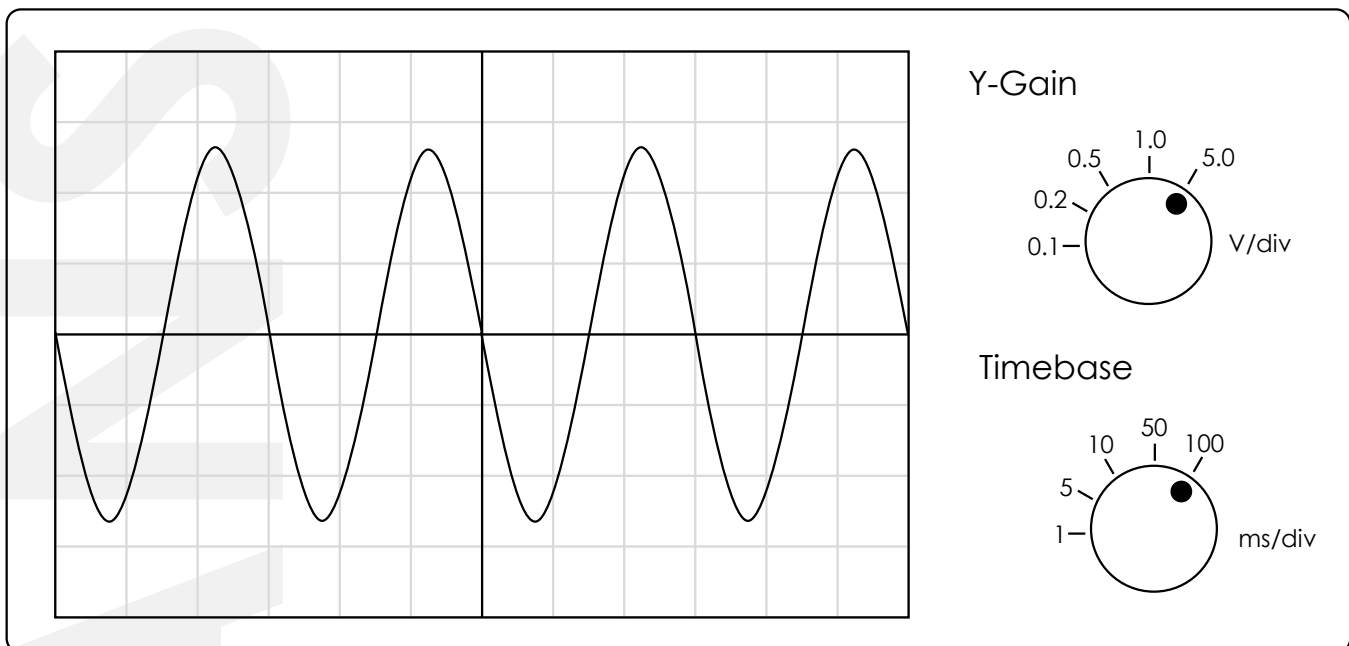
- a. Calculate the **percentage uncertainty** (to 2 s.f.) of this measurement

$$\frac{0.4}{88.3} = \underline{0.45\%}$$

- b. State the **percentage uncertainty** in the calculated wavelength of the standing wave

$$\rightarrow \underline{0.45\%}$$

3. Determine the **amplitude** (in V) and **frequency** of the signal on this oscilloscope trace:



$$A = 2.6 \times 5.0 = \underline{13V}$$

$$f = \frac{1}{T} = \frac{1}{3 \times 100 \times 10^{-3}} = \underline{3.3 \text{ Hz}}$$

1. Determine the **result** that should be recorded for the amplitude,  $A$ , and calculate the **percentage uncertainty** in the data:

A / cm	9.8	9.4	<del>6.1</del>	9.5	9.4
--------	-----	-----	----------------	-----	-----

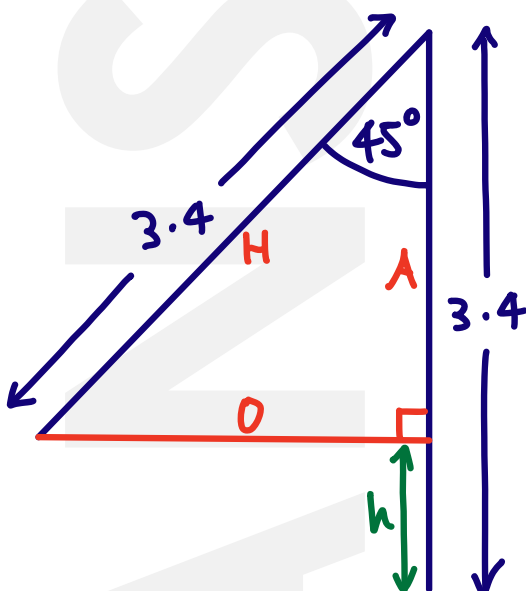
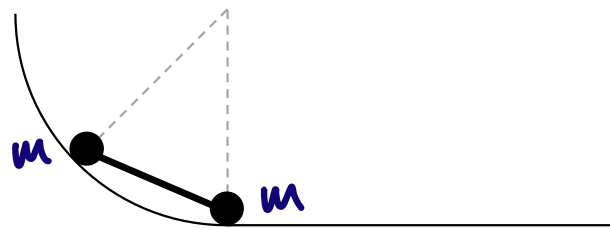
$$A = \underline{9.5 \text{ cm}}$$

$$\frac{0.2}{9.525} \times 100 = \underline{2.1\%}$$

2. A smooth surface consists of a quarter circle sheet joined onto a smooth horizontal plane. A light, rigid rod with two small, equal masses,  $m$ , on each end lies in a vertical plane with the lower mass on the join of the flat and curved surfaces, as shown in the figure below. The separation of the masses is  $1/8$  of the circumference of the circle.

When released, the rod and masses will slide along the smooth horizontal plane. Calculate the **maximum speed** if the rod and masses remain in the same vertical plane.

The radius of the circle is 3.4 m.



$$\cos \theta = \frac{A}{H}$$

$$A = H \cos \theta$$

$$A = 3.4 \cos 45$$

$$A = 2.404 \text{ m}$$

$$h = 3.4 - 2.404$$

$$h = 0.9958$$

$$E_p \rightarrow E_k$$

~~$$mgh = \frac{1}{2}(2m)v^2$$~~

$$gh = v^2$$

$$v = \sqrt{gh}$$

$$v = \sqrt{9.81 \times 0.9958}$$

$$v = \underline{3.1 \text{ m s}^{-1}}$$

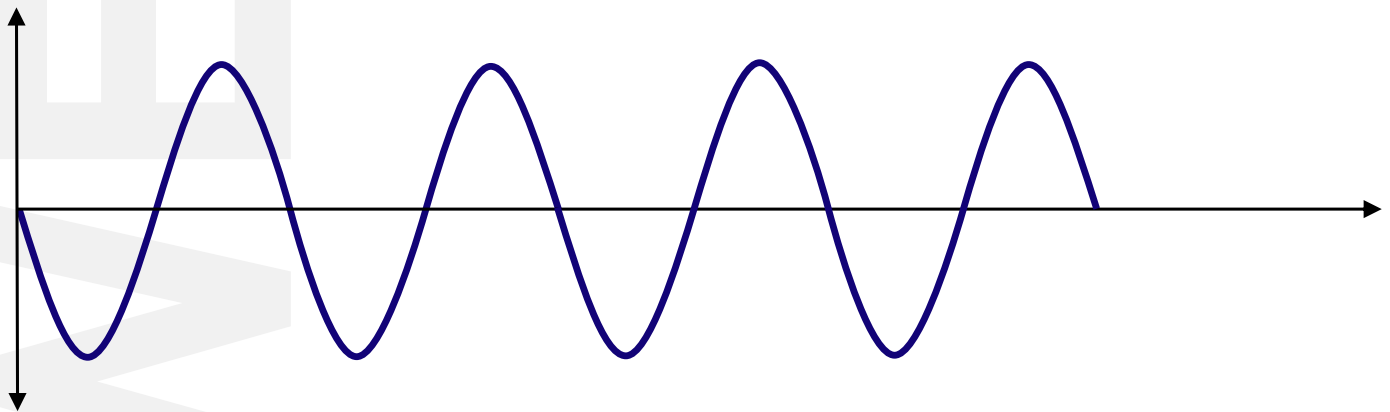
1. The diameter of a wire, used to measure the Young modulus of copper, was measured in three places with values of 0.42, 0.46 and 0.41 mm.

Calculate the **mean value** and **percentage uncertainty** (to 2 s.f.) of these measurements.

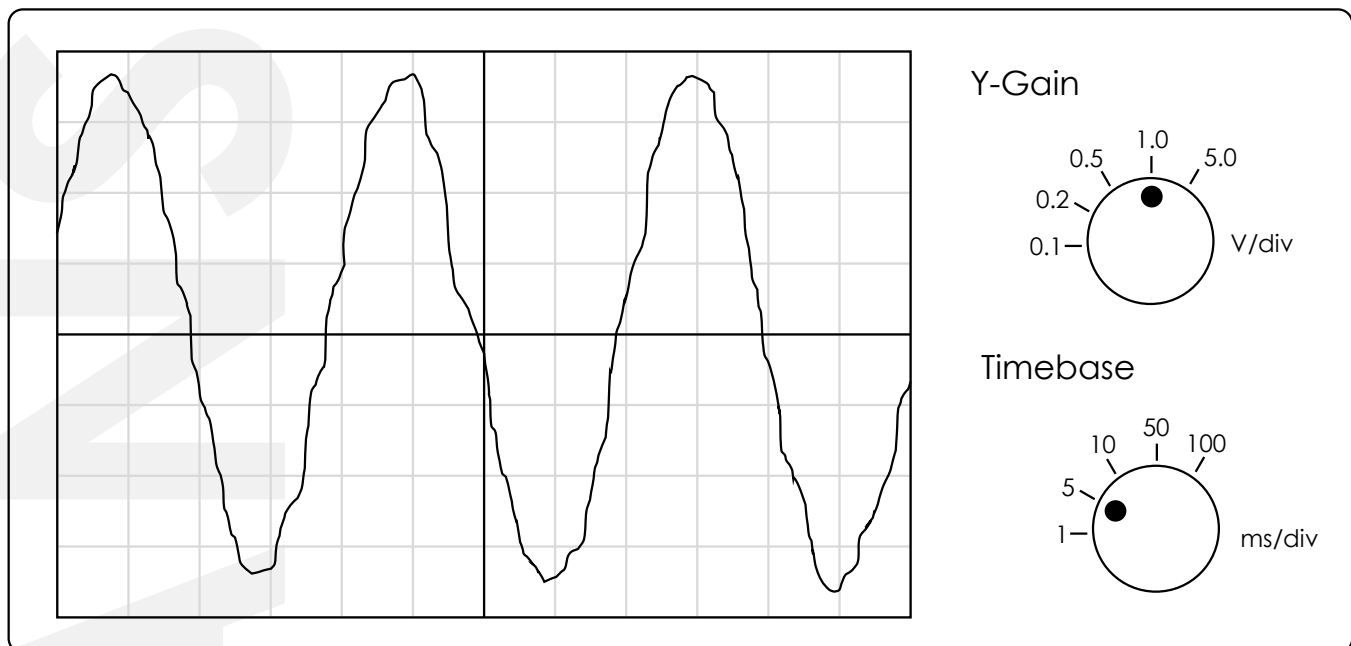
$$\frac{0.42 + 0.46 + 0.41}{3} = \underline{0.43 \text{ mm}}$$

$$\frac{0.025}{0.43} \times 100 = \underline{5.8\%}$$

2. Complete the following **sinusoidal** curve:



3. Determine the **amplitude** (in V) and **frequency** of the signal on this oscilloscope trace.



$$A = 3.8 \times 1.0 = \underline{3.8 \text{ V}}$$

$$f = \frac{1}{T} = \frac{1}{4.1 \times 5 \times 10^{-3}} = \underline{49 \text{ Hz}}$$

## Adding Uncertainties

The total uncertainty in a final value can be estimated by adding the absolute uncertainties in the measured values.

$$A = B + C \quad \Delta A = \Delta B + \Delta C$$

$$A = B - C \quad \Delta A = \Delta B + \Delta C$$

Note: The uncertainty here has been represented here by ' $\Delta X$ '. There is no standard for this at A Level and exam mark schemes give credit for all reasonable methods of working out.

1. The original length of a spring was 5.2 cm. After a tensile load was applied its final length is 8.3 cm. A ruler was used with an uncertainty of  $\pm 1$  mm.

- a. State the **absolute uncertainty** in each measurement

$$\pm 1 \text{ mm}$$

- b. Calculate the **extension** of the spring in mm

$$8.3 - 5.2 = 3.1 \text{ cm} \quad \text{or} \quad \underline{31 \text{ mm}}$$

- c. State the **total uncertainty** in the extension

$$\pm \underline{2 \text{ mm}}$$

- d. Calculate the **percentage uncertainty** (to 2 s.f.) in the extension of the spring

$$\frac{2}{31} \times 100 = \underline{6.5\%}$$

2. Write down the definition of **Hooke's law**.

$$F \propto x \quad (\text{provided the elastic limit is not exceeded})$$



1. The original length of a wire was 94.2 cm. After a tensile load was applied its final length was 97.1 cm. A ruler was used with an uncertainty of  $\pm 1$  mm.

a. State the **absolute uncertainty** in each measurement

$$\pm 1 \text{ mm}$$

b. Calculate the **extension** of the wire in mm

$$971 - 942 = \underline{29} \text{ mm}$$

c. State the **total uncertainty** in the extension

$$\pm \underline{2} \text{ mm}$$

d. Calculate the **percentage uncertainty** (to 2 s.f.) in the extension of the wire

$$\frac{2}{29} \times 100 = \underline{6.9\%}$$

2. Define:

a. Tensile **stress**

The force exerted per unit cross sectional area.

b. Tensile **strain**

The extension of an object divided by its original length.

c. The **Young modulus** of a material

The ratio of tensile stress to tensile strain.

1. Convert the following quantities into **SI units**:

- a. 630 nm  $6.30 \times 10^{-7} \text{ m}$   
b.  $82.3 \times 10^{-3} \text{ nm}$   $8.23 \times 10^{-11} \text{ m}$   
c. 568 ml  $5.68 \times 10^{-4} \text{ m}^3$   
d. 4.25 ly  $4.02 \times 10^{16} \text{ m}$   
e. 30.0 mph  $13.4 \text{ m s}^{-1}$

2. The time taken for a pendulum to make one oscillation was recorded as 0.8 s with an uncertainty estimated to be  $\pm 0.2 \text{ s}$  due to human error.

a. Calculate the **percentage uncertainty** (to 2 s.f.) in this measurement

$$\frac{0.2}{0.8} \times 100 = \underline{25\%}$$

To improve the experiment the time taken for ten oscillations was recorded. A value of 8.2 was recorded, with the same uncertainty of  $\pm 0.2 \text{ s}$  due to human error.

b. Calculate the **percentage uncertainty** (to 2 s.f.) in this measurement

$$\frac{0.2}{8.2} \times 100 = \underline{2.4\%}$$

The experiment was carried out by a different group. They recorded the following times from a stopwatch.

$t_{10} / \text{s}$	8.19	8.17	8.07	8.02	8.11
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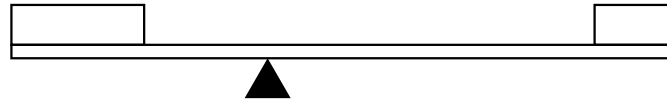
c. Calculate the **percentage uncertainty** (to 2 s.f.) in this set of data

$$\frac{0.085}{8.112} = \underline{1.0\%}$$

d. Comment on your answer

Percentage uncertainty reduces with repeated readings for multiple oscillations.

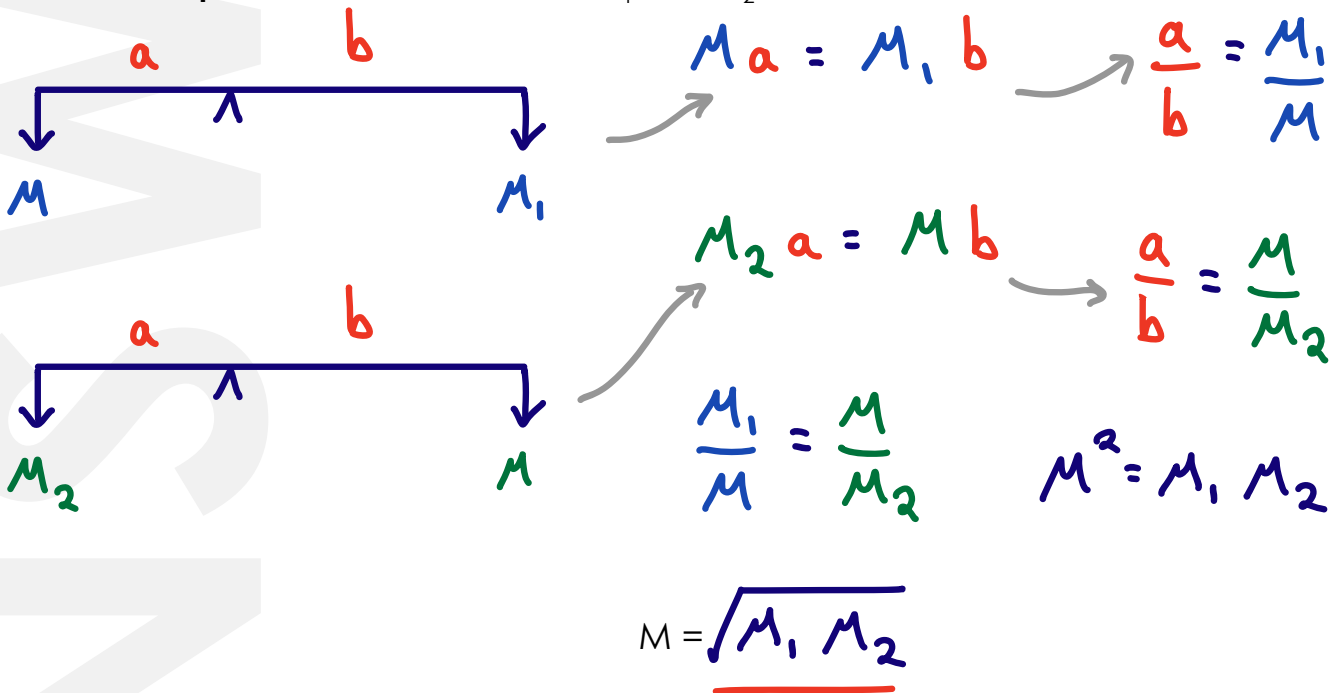
1. A lever balance, of the same type shown below, can be used to measure the mass of an object.



It consists of two small, unequal pans at the end of a beam balanced on a fulcrum. The arms of the balance are of unequal length, but the beam remains horizontal when the pans are not loaded.

An object of mass  $M$  is to be measured. When placed in one pan, the balance is levelled with a mass  $M_1$  in the other pan. When  $M$  is placed into other pan, it is balanced by a mass  $M_2$ .

- a. Find an **expression** that relates  $M$  to  $M_1$  and  $M_2$ .

Handwritten diagrams and equations for part a. The first diagram shows a beam with a fulcrum. The left arm has length 'a' and a downward arrow labeled 'M'. The right arm has length 'b' and a downward arrow labeled 'M1'. To the right, the equation  $M a = M_1 b$  is written, followed by an arrow pointing to  $\frac{a}{b} = \frac{M_1}{M}$ . The second diagram shows the same beam with a fulcrum. The left arm has length 'a' and a downward arrow labeled 'M2'. The right arm has length 'b' and a downward arrow labeled 'M'. To the right, the equation  $M_2 a = M b$  is written, followed by an arrow pointing to  $\frac{a}{b} = \frac{M}{M_2}$ . Below these, the equation  $\frac{M_1}{M} = \frac{M}{M_2}$  is written, followed by an arrow pointing to  $M^2 = M_1 M_2$ . At the bottom, the final expression  $M = \sqrt{M_1 M_2}$  is written, with the square root term underlined.

- b. If  $M_1 = 1.22$  kg and  $M_2 = 1.90$  kg, calculate the **value** of the mass  $M$ .

$$M = \sqrt{M_1 M_2} = \sqrt{1.22 \times 1.90} = \underline{1.52 \text{ kg}}$$

## Combining Uncertainties

The total percentage uncertainty in a calculated value can be estimated by combining the percentage uncertainties of the measured values.

$$A = BC \quad \%A = \%B + \%C$$

$$A = BCD \quad \%A = \%B + \%C + \%D$$

$$A = B/C \quad \%A = \%B + \%C$$

$$A = B^2 \quad \%A = 2 \times \%B$$

$$A = B^3 \quad \%A = 3 \times \%B$$

$$A = \sqrt{B} \quad \%A = \frac{1}{2} \times \%B$$

$$A = B^2C/D^3E \quad \%A = (2 \times \%B) + \%C + (3 \times \%D) + \%E$$

Note: The percentage uncertainty has been represented here by '%X', this can also be represented by '%U', '%uncertainty' or even 'ε'. There is no standard A Level symbol for this and exam mark schemes give credit for all reasonable methods of working out.

1. Measurements were made to determine the current and potential difference in a circuit component.

Quantity	Percentage Uncertainty
Current	1.8 %
Potential Difference	3.1 %

Calculate the **percentage uncertainty** in the calculated value of:

- a. **Resistance**

$$R = V/I$$

$$\%R = \%V + \%I = 3.1 + 1.8 = \underline{4.9\%}$$

- b. **Power**

$$P = VI$$

$$\%P = \%V + \%I = 3.1 + 1.8 = \underline{4.9\%}$$

# 19<sup>th</sup> November – Part 2

2

3

2. Measurements were made to determine the current, potential difference and time in an electrical circuit with a heater.

Quantity	Percentage Uncertainty
Current	4.7 %
Potential Difference	1.7 %
Time	0.2 %

Calculate the **percentage uncertainty** in the calculated value of:

- a. **Resistance**

$$R = V/I$$

$$\%R = \%V + \%I = 1.7 + 4.7 = \underline{6.4\%}$$

- b. **Energy transferred**

$$E = ItV$$

$$\%E = \%I + \%t + \%V = 4.7 + 0.2 + 1.7 = \underline{6.6\%}$$

3. Measurements were made to determine the diameter, length and resistance of a wire.

Quantity	Percentage Uncertainty
Diameter	2.2 %
Length	0.6 %
Resistance	1.3 %

$$\rho = \frac{RA}{l}$$

Calculate the **percentage uncertainty** in the calculated value of **resistivity**.

$$\% \rho = \%R + \%A + \%L = 1.3 + (2 \times 2.2) + 0.6 = \underline{6.3\%}$$

$$\%A = 2 \times \%d$$

1. Determine the **result** that should be recorded for M and calculate the **percentage uncertainty** in the data:

M / kg	0.098	0.101	0.100	0.104	0.098
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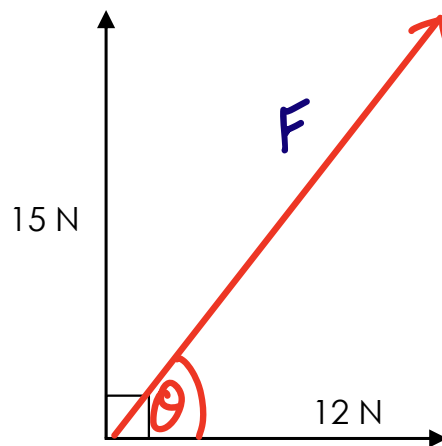
$$M = \underline{0.100 \text{ kg}}$$

$$\frac{0.003}{0.1002} \times 100 = \underline{3.0\%}$$

2. Calculate the **size** and **direction** of the resultant force produced by these two perpendicular forces.

$$F = \sqrt{12^2 + 15^2}$$

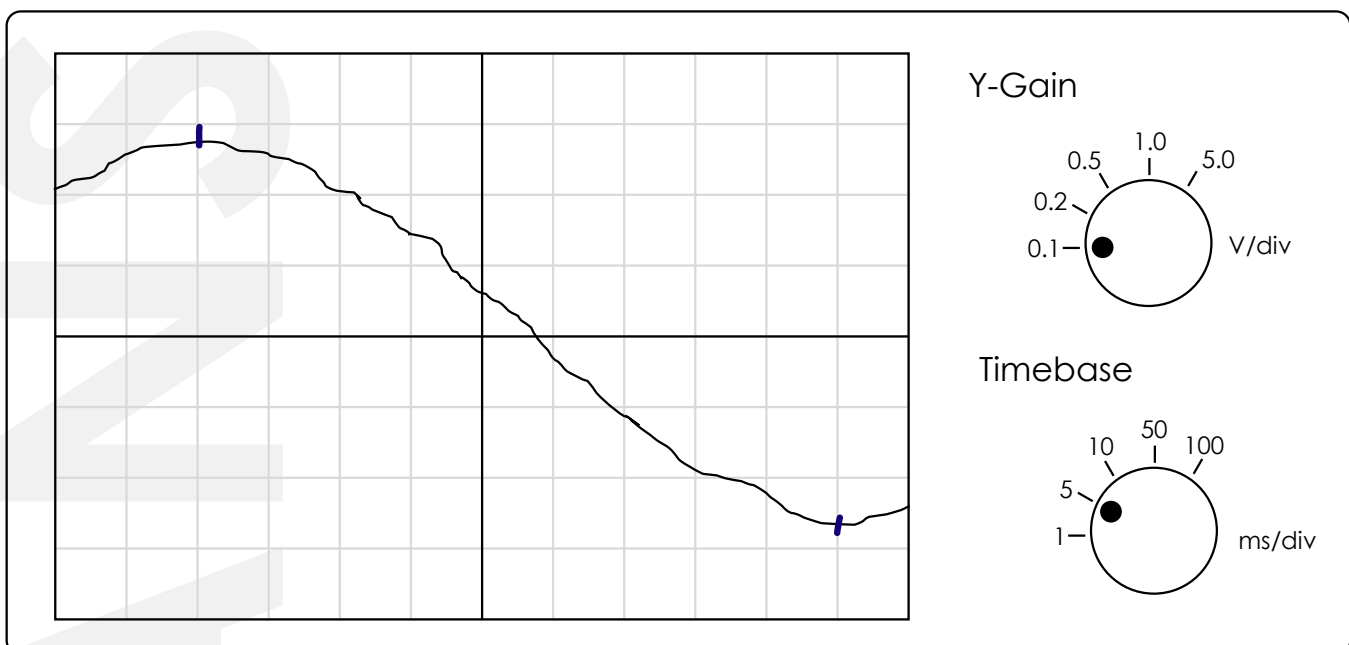
$$F = 19.2 \approx \underline{19 \text{ N}}$$



$$\theta = \tan^{-1}\left(\frac{15}{12}\right) = 51.3$$

$$\theta = \underline{51^\circ}$$

3. Determine the **amplitude** (in V) and **frequency** of the signal on this oscilloscope trace.



$$A = 2.8 \times 0.1 = \underline{0.28 \text{ V}}$$

$$f = \frac{1}{T} = \frac{1}{9 \times 2 \times 5 \times 10^{-3}} = \underline{11 \text{ Hz}}$$

1. Define:

a. **Plastic** behaviour

A material has a permanent change of shape when the load is removed.

b. **Elastic** behaviour

Material returns to its original dimensions when the load is removed.

2. The resistance of a wire is proportional to its length  $l$ , and inversely proportional to its cross-sectional area  $A$ . The constant of proportionality,  $\rho$ , is known as the resistivity of the material.

$$R = \frac{\rho l}{A}$$

For copper, the resistivity  $\rho_{\text{Cu}} = 1.68 \times 10^{-8} \Omega \text{ m}$  and for silicon, a semiconductor, with trace amounts of impurities,  $\rho_{\text{Si}} = 0.53 \Omega \text{ m}$ .

The resistance between two opposing faces of a copper cube of length 1.00 m and cross-sectional area 1.00 m<sup>2</sup> is  $1.68 \times 10^{-8} \Omega$ .

Calculate the **length** of the side of a **cube** of silicon with if it had a resistance of  $1.68 \times 10^{-8} \Omega$  between opposite faces.

$$V = l^3 \quad A = l^2$$

$$R = \frac{\rho l}{A} = \frac{\rho l}{l^2} = \frac{\rho}{l}$$

$$l_{\text{Si}} = \frac{\rho_{\text{Si}}}{R_{\text{Si}}} = \frac{0.53}{1.68 \times 10^{-8}} = \underline{3.15 \times 10^7 \text{ m}}$$

1. Measurements were made to determine the force on a wire perpendicular to a magnetic field. Calculate the **percentage uncertainty** in the calculated value based on these measurements.

Quantity	Percentage Uncertainty
Magnetic field strength	5.0 %
Current	2.1 %
Length	0.3 %

$$F = BIL$$

$$\%F = \%B + \%I + \%L$$

$$= 5.0 + 2.1 + 0.3$$

$$= \underline{7.4\%}$$

2. Rearrange the following equation to make 'k' the subject:  $T = 2\pi\sqrt{\frac{m}{k}}$

$$T = 2\pi\sqrt{\frac{m}{k}}$$

$$T^2 = 4\pi^2 \frac{m}{k}$$

$$k = 4\pi^2 \frac{m}{T^2}$$

3. Sketch the **standing/stationary** wave formed on a **string** fixed at both ends:

a. First harmonic



b. Second harmonic



c. Third harmonic



d. Fourth harmonic





1. Measurements were made to determine the spring constant on an oscillating mass-spring system. Calculate the **percentage uncertainty** in the calculated value of 'k' based on these measurements.

Quantity	Percentage Uncertainty
Mass	0.2 %
Time period	1.3 %

$$T = 2\pi \sqrt{\frac{m}{k}}$$

$$k = 4\pi^2 \frac{m}{T^2} \quad \%k = \%m + (2 \times \%T) = 0.2 + (2 \times 1.3) = \underline{2.8\%}$$

2. Rearrange the following equation to make 'g' the subject:  $T = 2\pi \sqrt{\frac{l}{g}}$

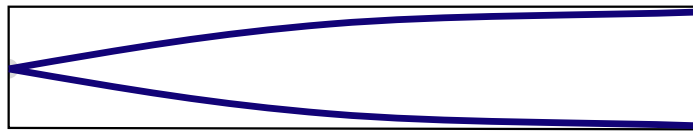
$$T = 2\pi \sqrt{\frac{l}{g}}$$

$$T^2 = 4\pi^2 \frac{l}{g}$$

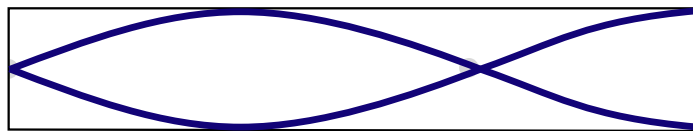
$$g = 4\pi^2 \frac{l}{T^2}$$

3. Sketch the **standing/stationary** wave formed in the tube open at one end:

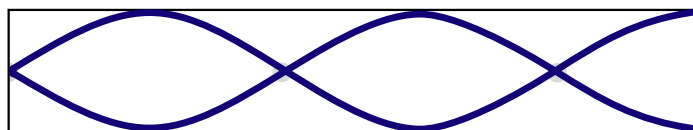
a. First harmonic



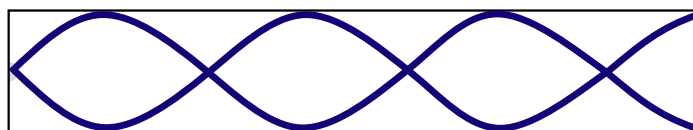
b. Second harmonic



c. Third harmonic



d. Fourth harmonic



1. Measurements were made to determine the gravitational field strength using an oscillating pendulum. Calculate the **percentage uncertainty** in the calculated value of 'g' based on these measurements.

Quantity	Percentage Uncertainty
Length	1.0 %
Time period	2.3 %

$$T = 2\pi \sqrt{\frac{l}{g}}$$

$$g = 4\pi^2 \frac{l}{T^2} \quad \%g = \%L + (2 \times \%T) = 1.0 + (2 \times 2.3) = \underline{5.6\%}$$

2. Rearrange  $F = 6\pi\eta rv$  to make:

a. **r** the subject

$$r = F / 6\pi\eta v$$

b. **v** the subject

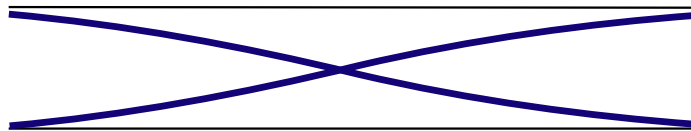
$$v = F / 6\pi\eta r$$

c. **η** the subject

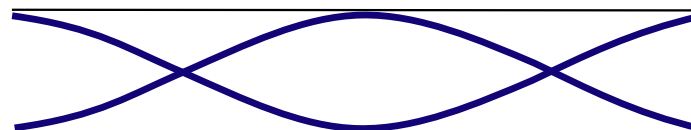
$$\eta = F / 6\pi r v$$

3. Sketch the **standing/stationary** wave formed in a tube open at both ends:

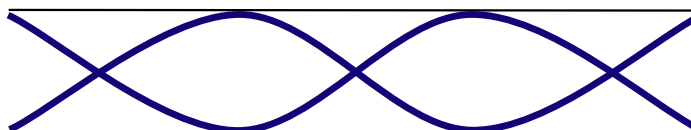
a. First harmonic



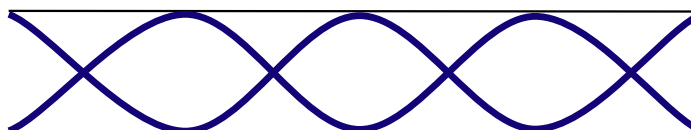
b. Second harmonic



c. Third harmonic

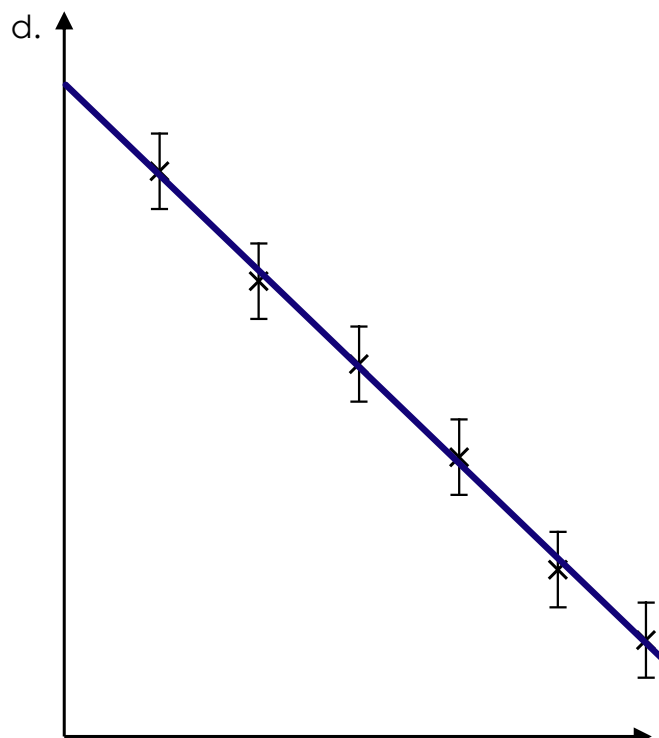
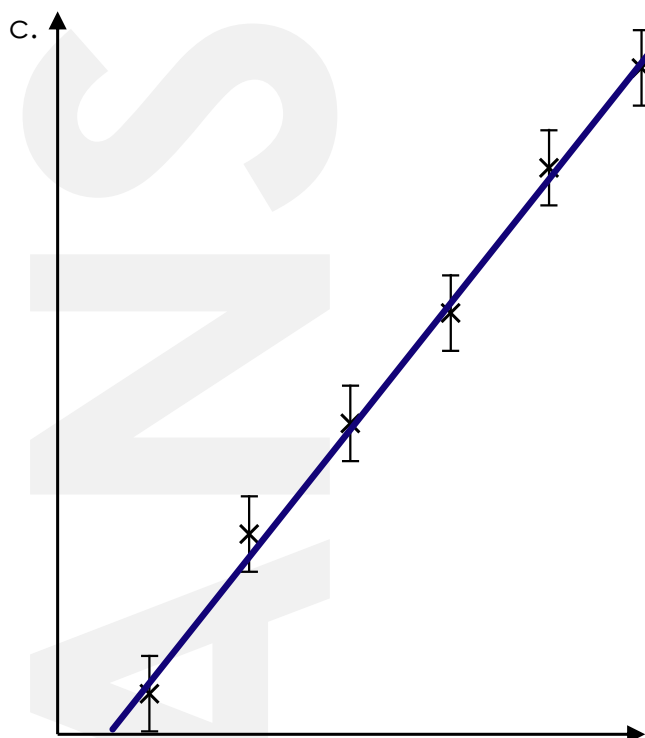
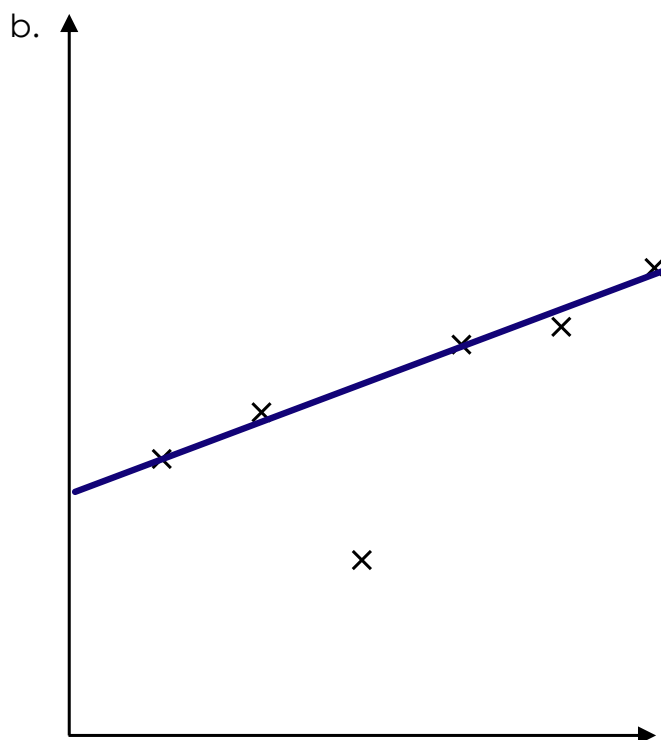
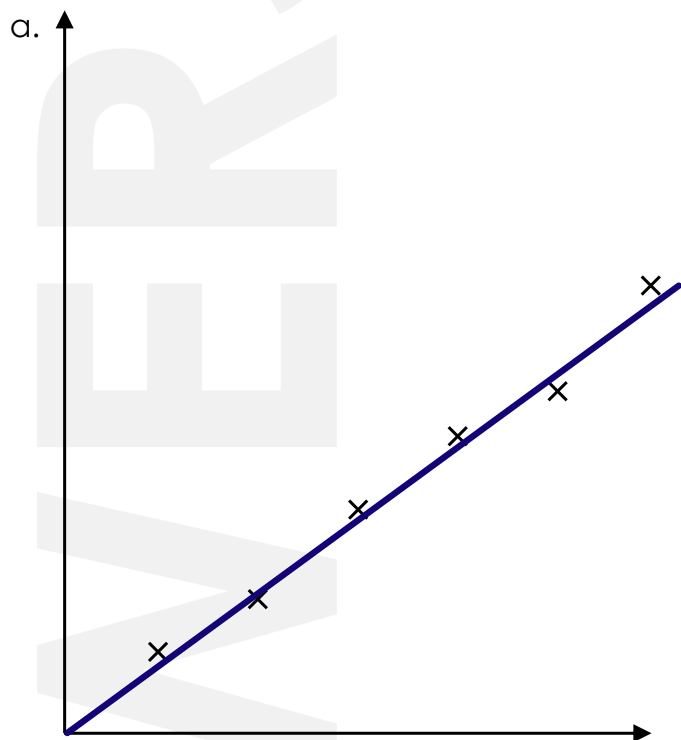


d. Fourth harmonic



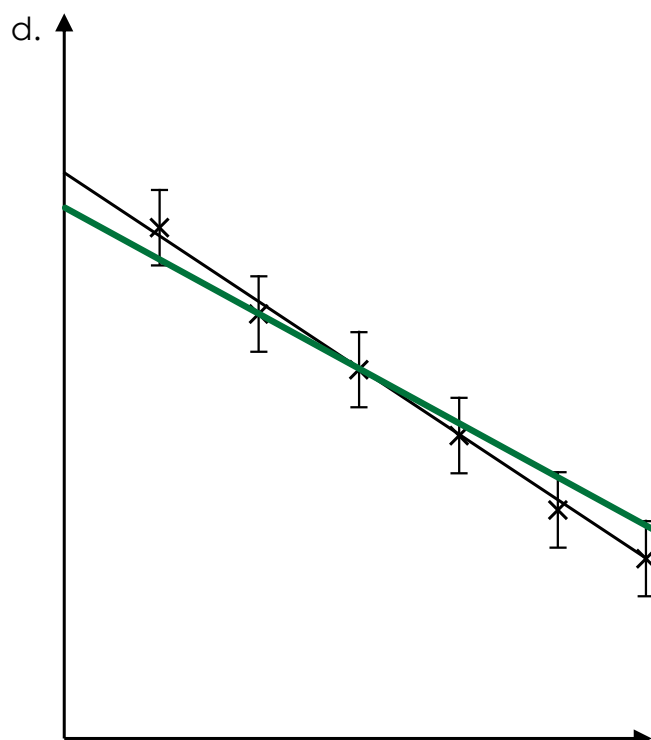
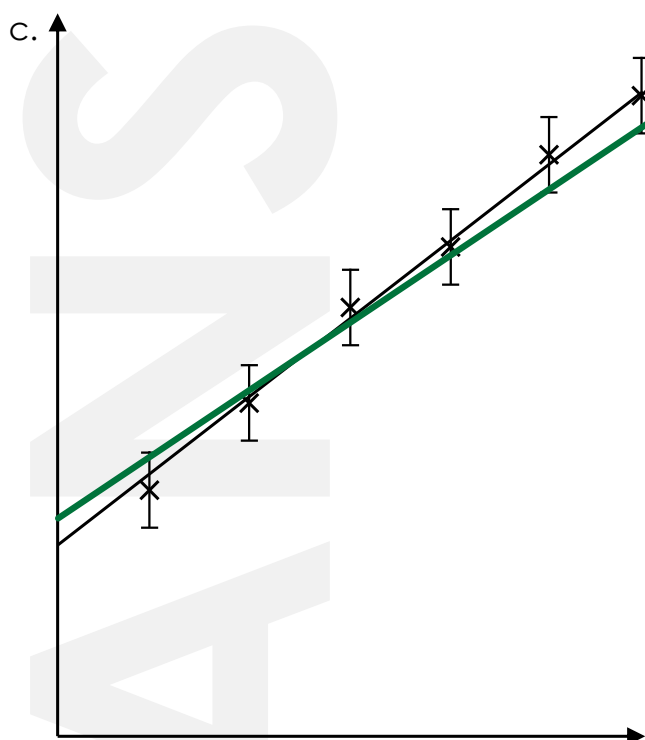
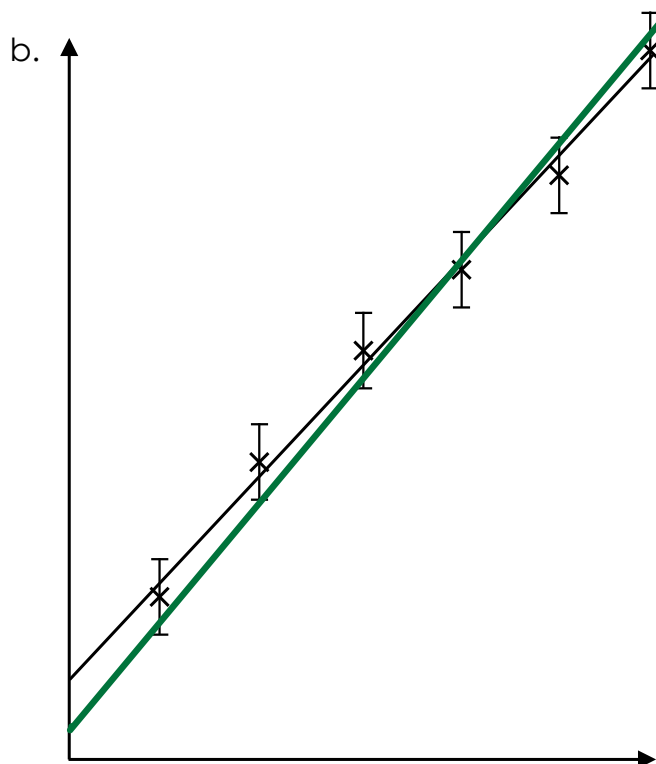
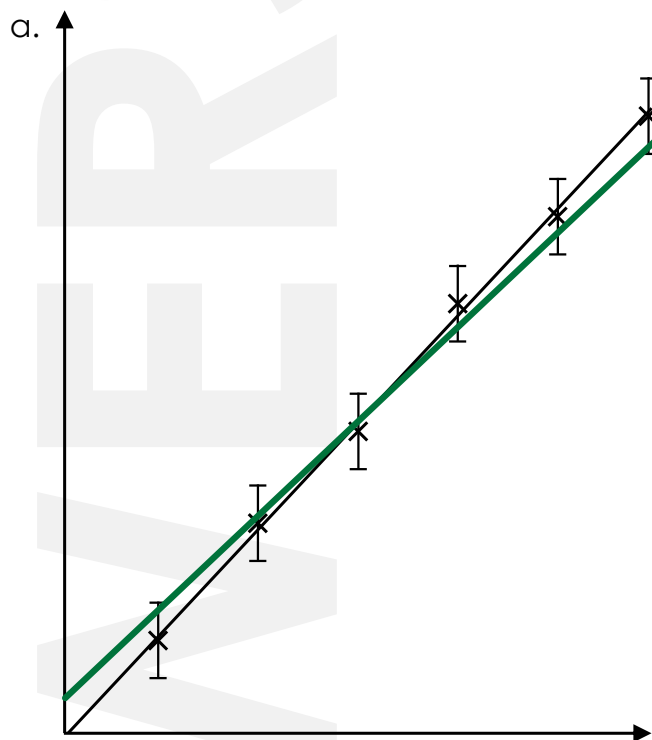
# 25<sup>th</sup> November – Part 1

1. Draw in a straight **line of best fit** for the following data:



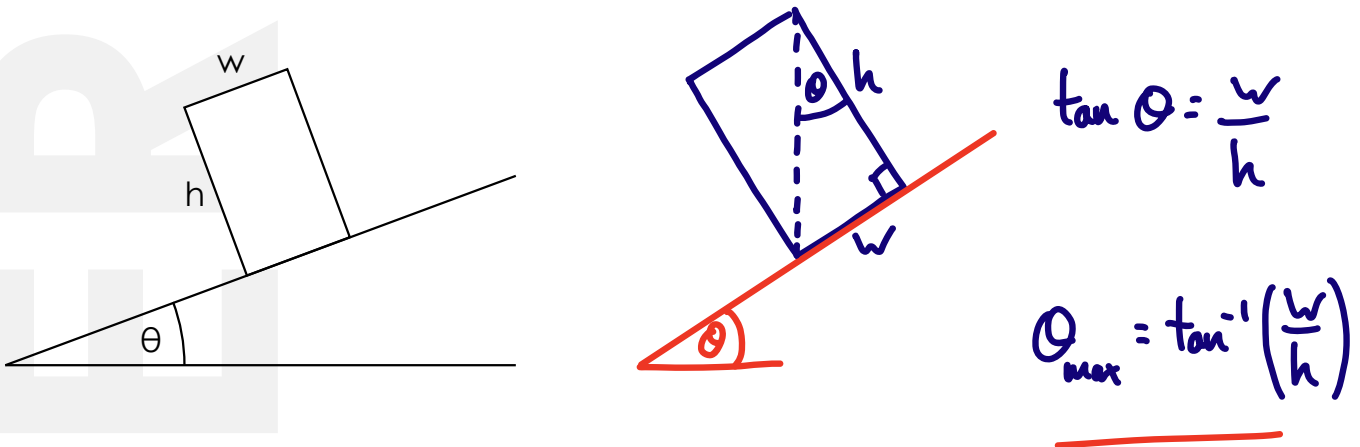
# 25<sup>th</sup> November – Part 2

2. The 'line of best fit' has been added to these graphs. Draw in a '**worst acceptable**' line. This must pass through all the error bars for the following data.



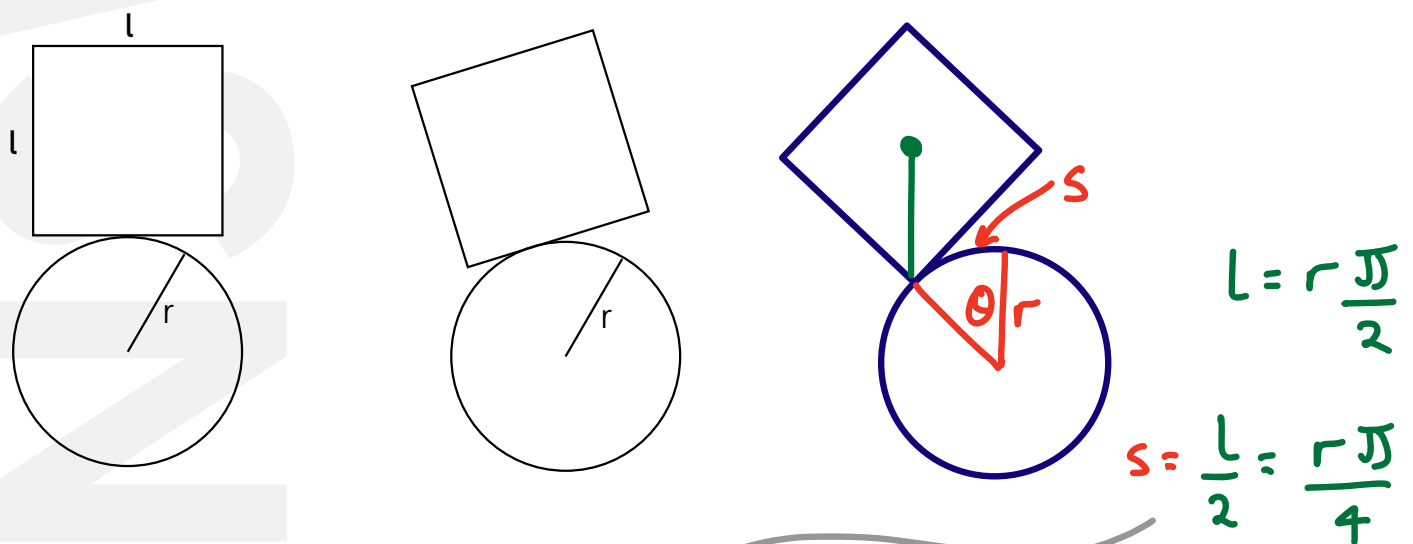
1. A solid rectangular block of height 'h' and width 'w' is placed on a plane inclined at an angle  $\theta$ . Friction prevents the block from sliding down the slope.

Write down an expression for the **maximum angle** of the slope ' $\theta_{\max}$ ' such that the block will remain upright.



From a BPhO question from the 2015 Year 12 Challenge

2. A massive solid cube of side  $l = r\pi/2$ , and of uniform density, is placed on the highest point of a cylinder of radius  $r$ , as shown below. If the cylinder is rough so that no sliding occurs, calculate the full **range** of the **angle** through which the block can swing (or wobble) without tipping off (you can assume that this range of equilibrium positions is stable).



$$\theta = \frac{s}{r} = \frac{r\pi/4}{r} = \frac{\pi}{4} \text{ rad} = 45^\circ$$

Full angle =  $\frac{\pi}{2}$  rad or  $90^\circ$

From a BPhO question from the 2015 Year 12 Challenge

1. Write the following derived units in terms of their SI Base Units:

a. Coulomb

$$Q = It$$

$$C = [A] \times [s] = \underline{[As]}$$

b. Newton

$$F = ma$$

$$N = [kg] \times [ms^{-2}] = \underline{[kgms^{-2}]}$$

c. Joule

$$W = Fs$$

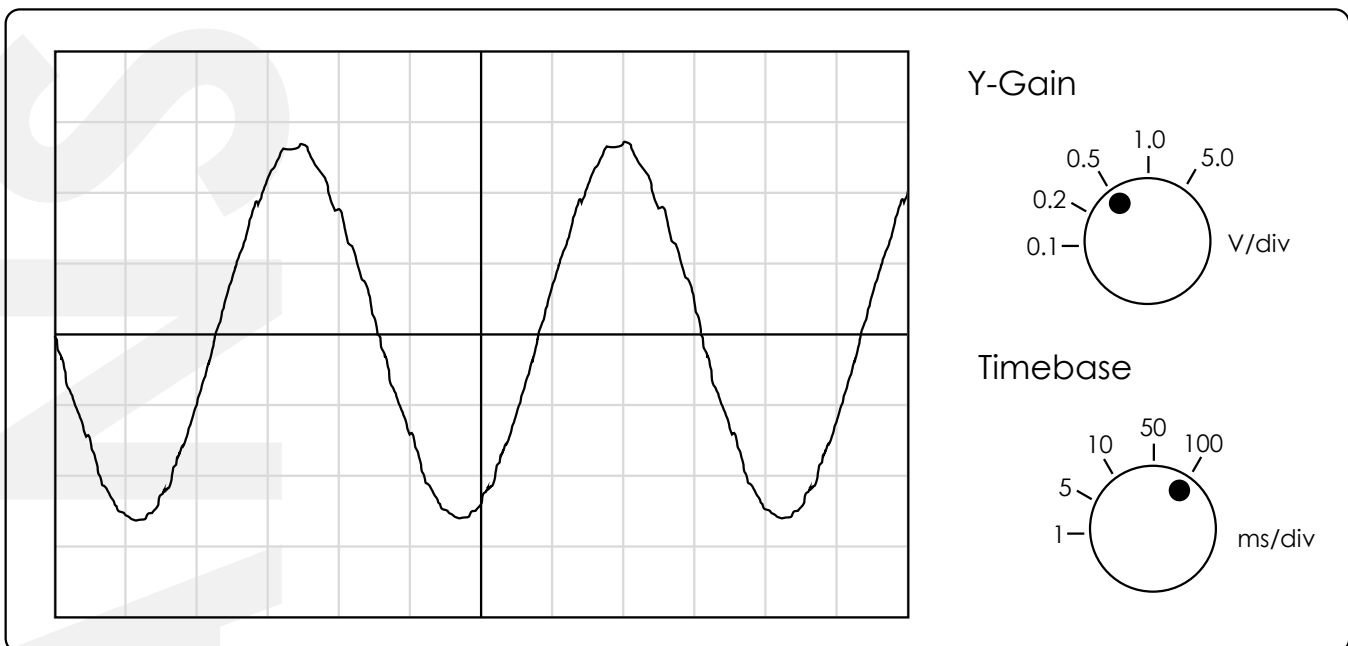
$$J = [kgms^{-2}] \times [m] = \underline{[kgm^2s^{-2}]}$$

d. Volt

$$V = W/Q$$

$$V = \frac{[kgm^2s^{-2}]}{[As]} = \underline{[kgm^2s^{-3}A^{-1}]}$$

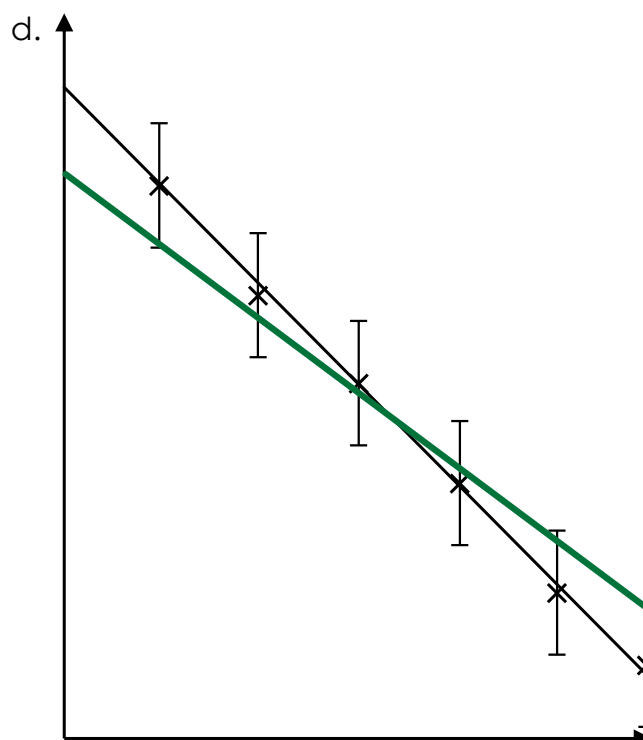
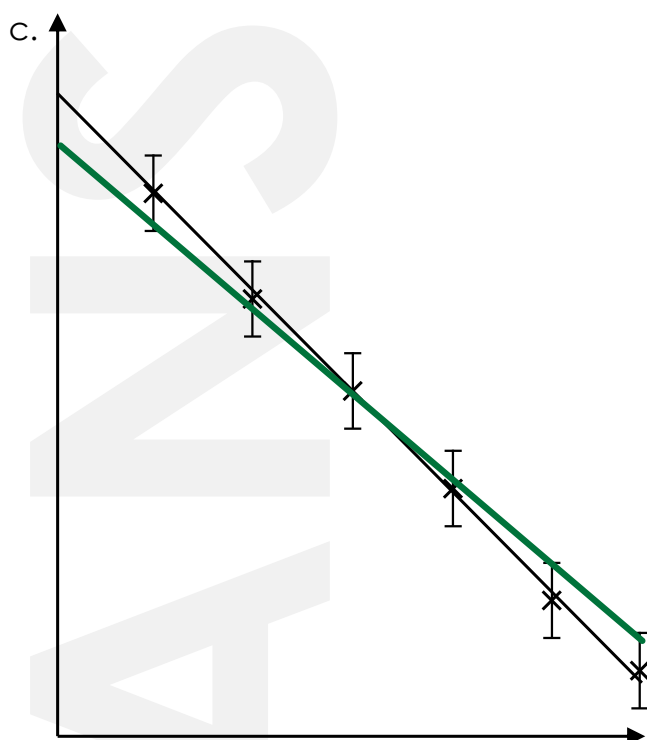
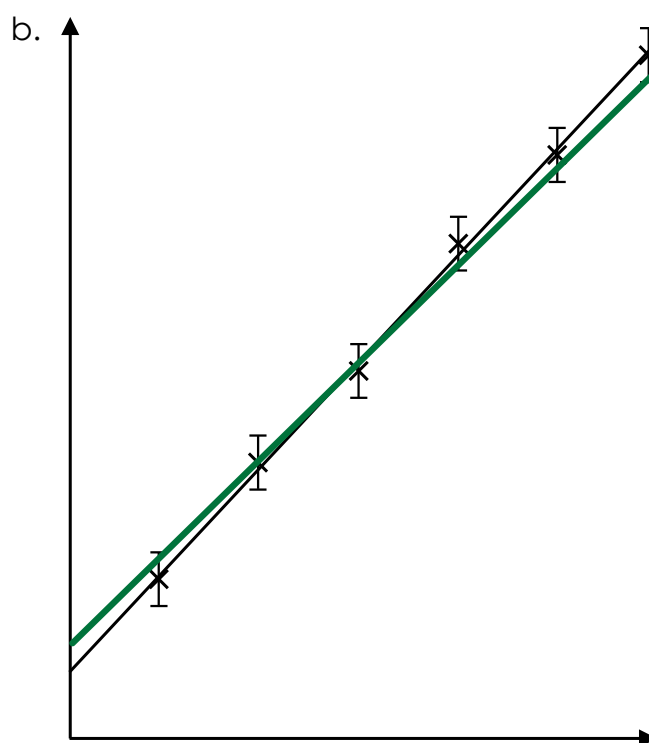
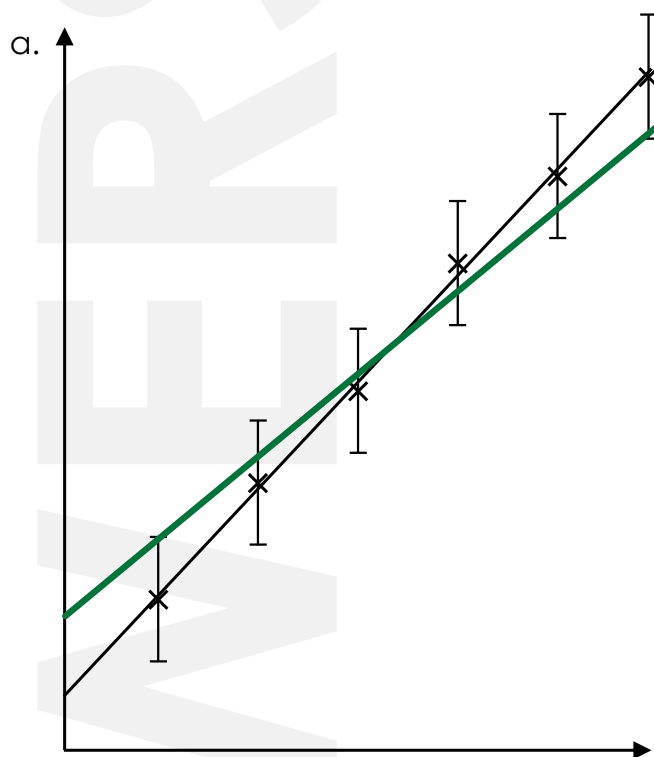
2. Determine the **amplitude** (in V) and **frequency** of the signal on this oscilloscope trace.



$$A = 2.8 \times 0.5 = \underline{1.4 \text{ V}} \quad f = \frac{1}{T} = \frac{1}{4.5 \times 100 \times 10^{-3}} = \underline{2.2 \text{ Hz}}$$

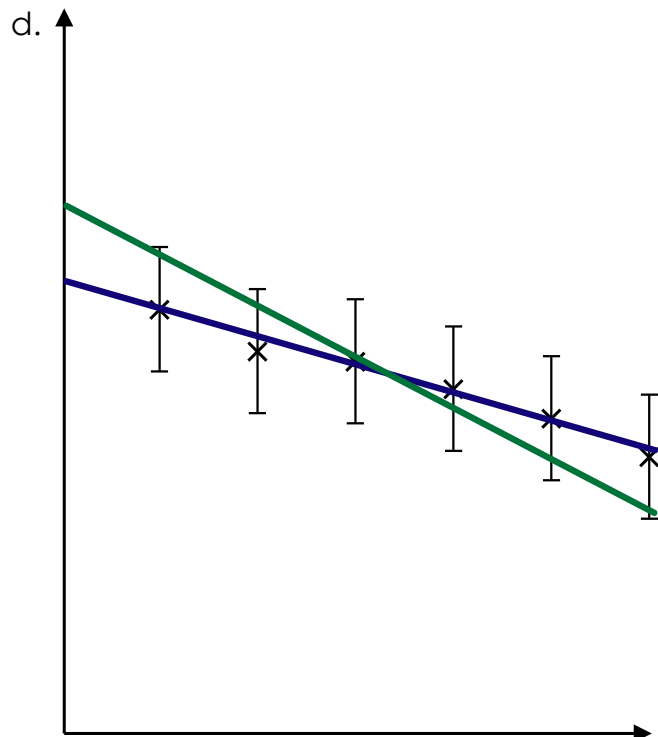
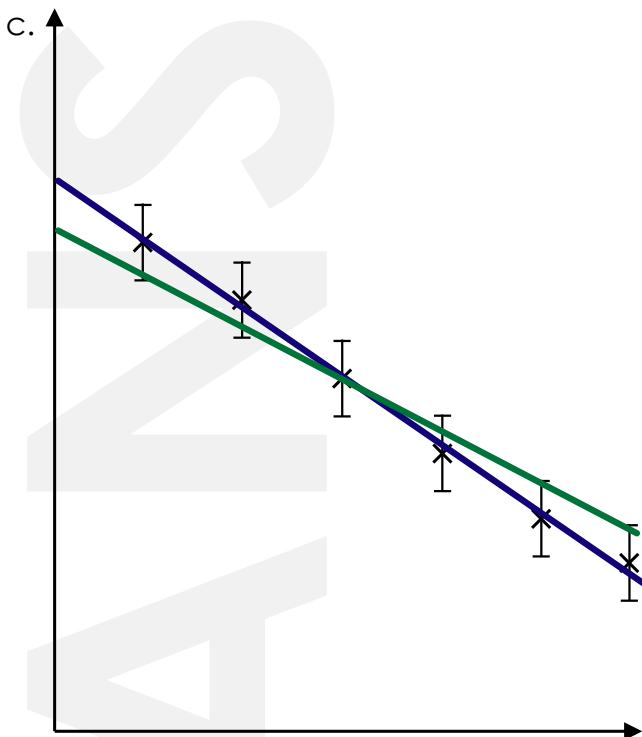
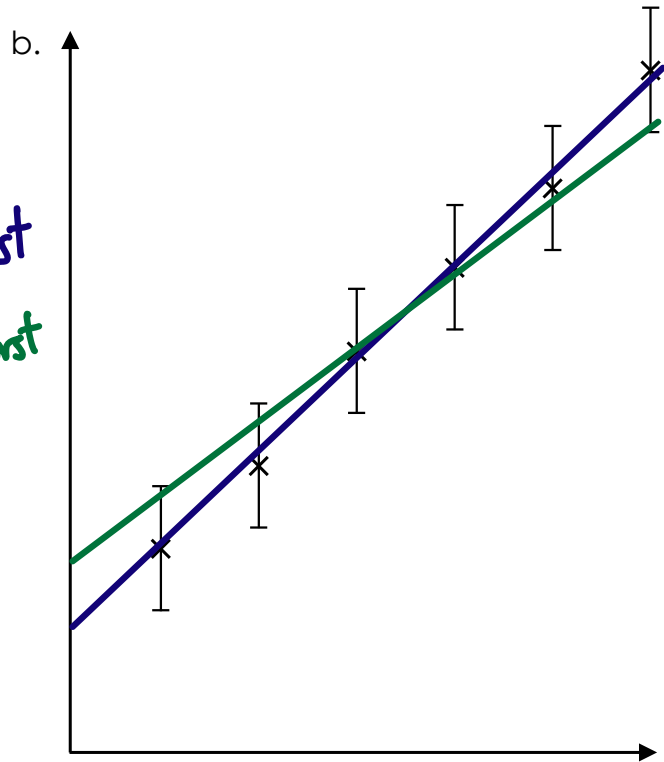
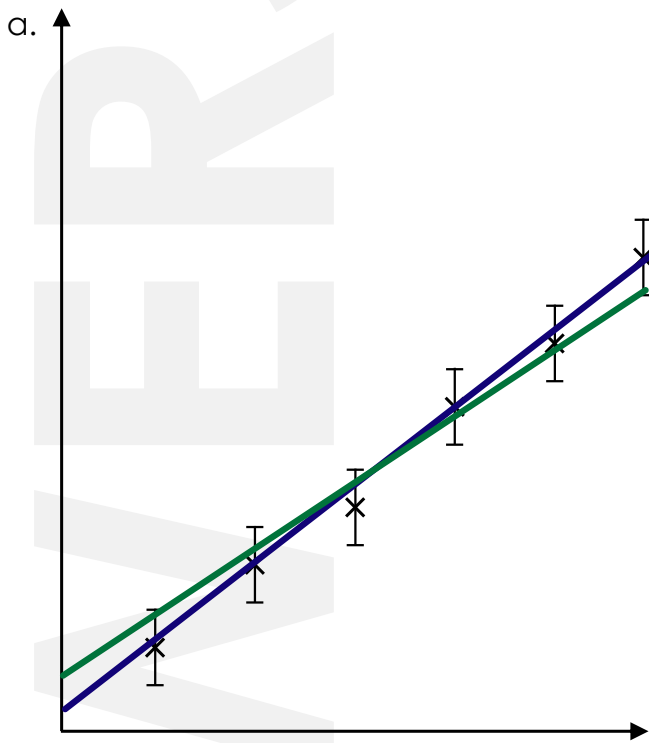
# 28<sup>th</sup> November – Part 1

1. Draw in a '**worst acceptable**' line. This must pass through the error bars for the following data:



# 28<sup>th</sup> November – Part 2

2. Draw in a 'line of best fit' and a 'worst acceptable' line that passes through the error bars for the following data:





1. A simple experiment is carried out to find the acceleration due to gravity 'g' by a freefall method. A ball is released from rest through a height measured as 80.0 cm with an uncertainty of  $\pm 1$  mm.

The following times are recorded with a digital stopwatch.

t / s	0.41	0.44	0.40	0.47	0.43
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- a. Calculate the **mean value** of 't'

$$\underline{0.43 \text{ s}}$$

- b. If air resistance is assumed to be negligible, calculate the **value** of 'g' that this data suggests

$$s = 0.800 \text{ m}$$

$$u = 0$$

$$v = 0$$

$$a = g$$

$$t = 0.43$$

$$s = \cancel{ut} + \frac{1}{2} at^2$$

$$g = \frac{2s}{t^2} = \frac{1.600}{0.43^2} = 8.653 = \underline{8.7 \text{ m s}^{-2}}$$

- c. Calculate the **percentage uncertainty** in the recorded data for height and time

$$s: \frac{1}{800} \times 100 = \underline{0.13\%}$$

$$t: \frac{0.035}{0.43} \times 100 = \underline{8.1\%}$$

- d. Calculate the **percentage uncertainty** in your final calculated value of 'g'

$$\%g = \%s + (2 \times \%t) = 0.125 + (2 \times 8.14) = 16.4 \approx \underline{16\%}$$

- e. Calculate the **uncertainty** (in  $\text{m s}^{-2}$ ) in your value for 'g'

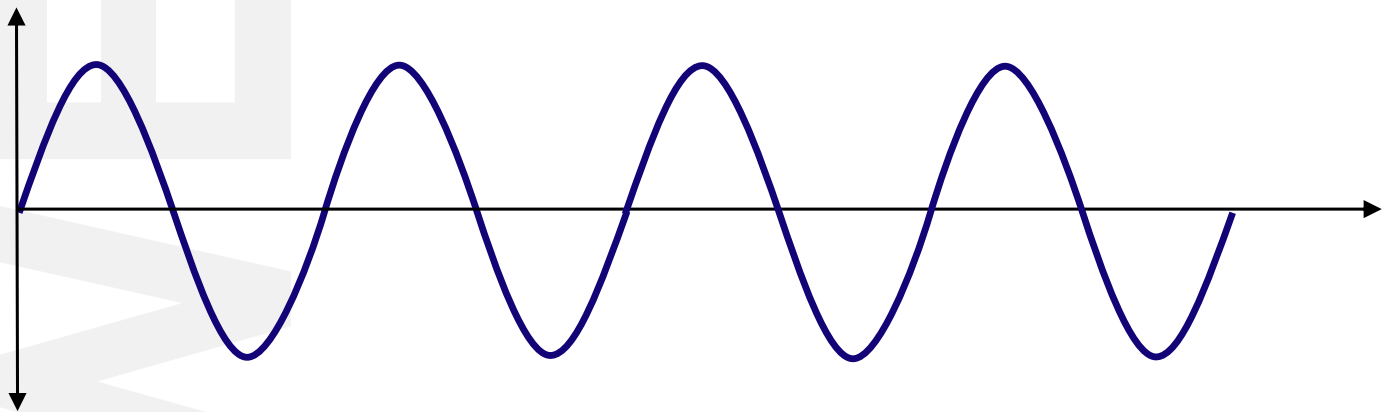
$$8.653 \times 0.164 = 1.42$$

$$\therefore \underline{\pm 1.4 \text{ m s}^{-2}}$$

1. Define **equilibrium**.

When the resultant force and moment on an object is zero.

2. Complete the following **sinusoidal** curve:

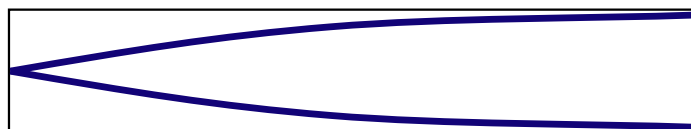


3. Sketch the fundamental frequency of **standing** wave formed below:

a. **String** fixed at both ends



b. Tube open at **one** end



c. Tube open at **both** ends

