



Please note: these solutions are not endorsed by Isaac Physics!

If you want to improve your understanding of the underlying physics then **you** have to work through the questions in the Linking Concepts book from Isaac Physics. There are answers in the back of the book for Question 1 and you can check your other answers by entering them at [isaacphysics.org](http://isaacphysics.org). This is just an example of how to work through a chapter.

Objects rising and falling exchange stores of gravitational potential and kinetic energy.

Example context: We can calculate the speed of objects after they have fallen. We can also work out the height to which a projected object rises. The analysis is particularly useful when balls bounce.

Quantities:	$h_0$	starting height (m)	$v_0$	starting speed (m s <sup>-1</sup> )
	$h_1$	final height (m)	$v_1$	final speed (m s <sup>-1</sup> )
	$m$	mass (kg)	$g$	gravitational field strength (N kg <sup>-1</sup> )
	$E_K$	kinetic energy (J)	$E_{GP}$	gravitational potential energy (J)
	$\eta$	efficiency (no unit)	$E_T$	total energy (J)

Equations:  $E_K = \frac{1}{2} m v^2$        $E_{GP} = m g h$        $E_T = E_K + E_{GP}$        $E_{T,after} = \eta E_{T,before}$

1.1 In the absence of air resistance, use the above equations to derive expressions for:

a. the speed  $v_1$  at the ground if an object was dropped from  $h_0$ .

b. the speed  $v_1$  at a height  $h_1$  if an object had speed  $v_0$  at  $h_0$ .

c. the greatest height  $h_1$  for an object projected up from the ground with speed  $v_0$ .

d. the greatest height  $h_1$  for an object projected up from a height  $h_0$  with speed  $v_0$ .

e. the greatest height  $h_1$  above a hard surface reached by an object dropped from a height  $h_0$  if the efficiency of the bounce is  $\eta$ .

f. the speed  $v_1$  just after a bounce from a hard surface if the speed just before was  $v_0$  (if the efficiency of the bounce is  $\eta$ ).

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1.2 An 800 kg pumpkin falls from 3.4 m. Calculate its speed just before striking the ground.

1.3 A 60 g tennis ball is hit upwards at  $27 \text{ m s}^{-1}$ . How high will it rise?

1.4 A 60 g tennis ball is hit upwards at  $27 \text{ m s}^{-1}$  from a 25 m rooftop. How fast will it be travelling when it passes the rooftop on the way down?

1.5 A 3.1 kg brick falls from scaffolding on a building site. A worker 3.5 m above the ground sees it fall past at  $6.5 \text{ m s}^{-1}$ . What is its kinetic energy just before striking the ground?

1.6 At what speed will a 4.2 kg lump of clay hit a potter's wheel if it is thrown downwards at  $1.1 \text{ m s}^{-1}$  from a height 40 cm above the wheel?

1.7 A worker at ground level throws a 2.2 kg drinks bottle upwards to a thirsty colleague 3.2 m above the ground. It just reaches him, but he fails to catch it, and it falls into an excavated trench 1.6 m below ground level.

a. At what speed did the worker need to throw the bottle if she threw it from the waist, 1.0 m above the ground?

b. How fast was it moving when it struck the base of the trench?

1.8 A 5.2 g ball is dropped from 90 cm onto a surface and bounces to a maximum height of 41 cm. Calculate the efficiency,  $\eta$ .

1.9 How fast would the ball, in question 1.8 above, rebound if it struck the surface at  $2.5 \text{ m s}^{-1}$ ?

1.10 How high would a ball bounce if it struck an  $\eta = 0.75$  surface at  $13 \text{ m s}^{-1}$ ?